

Experiment Simulation

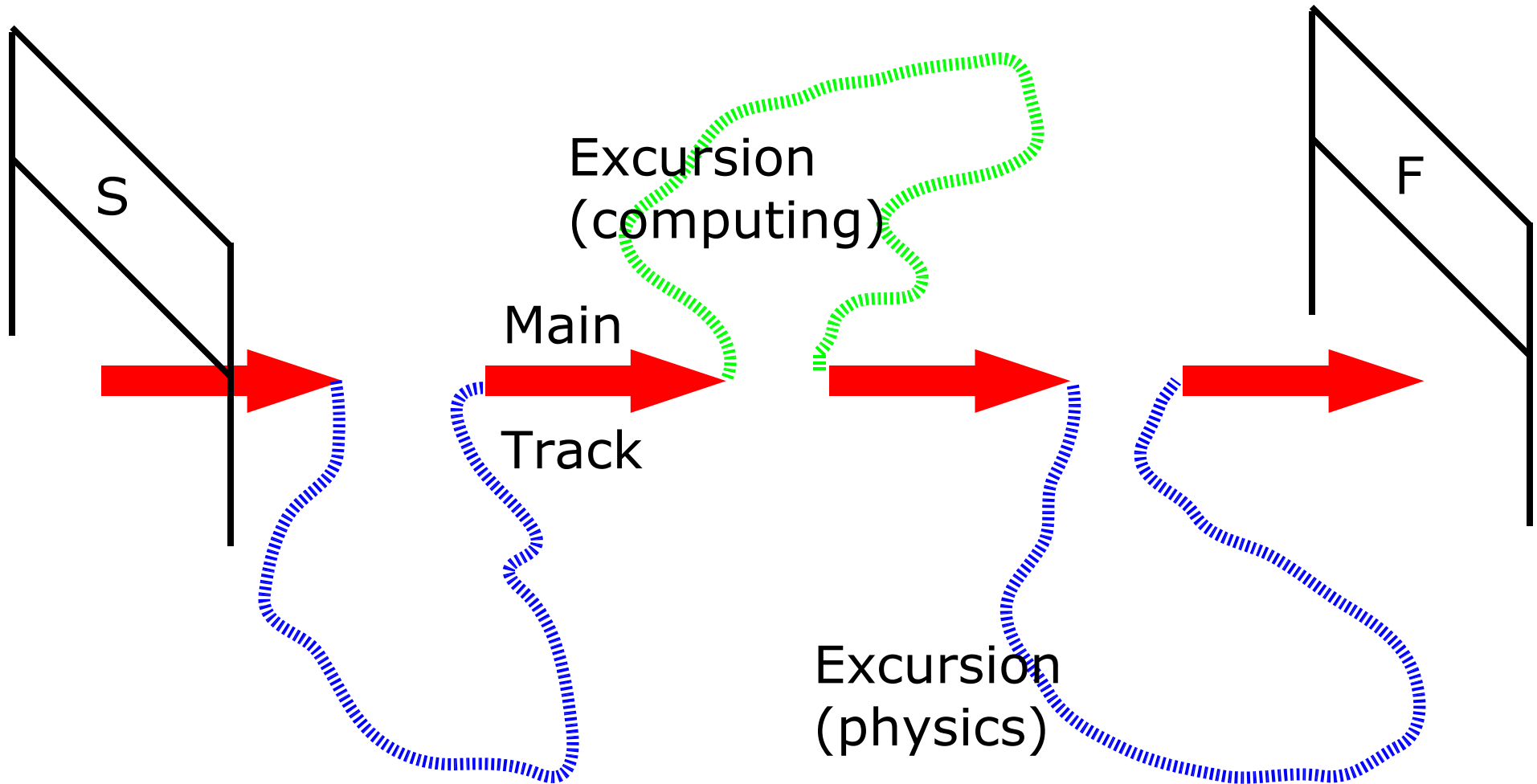
CERN School of Computing 2005
Saint Malo

Lecture 1

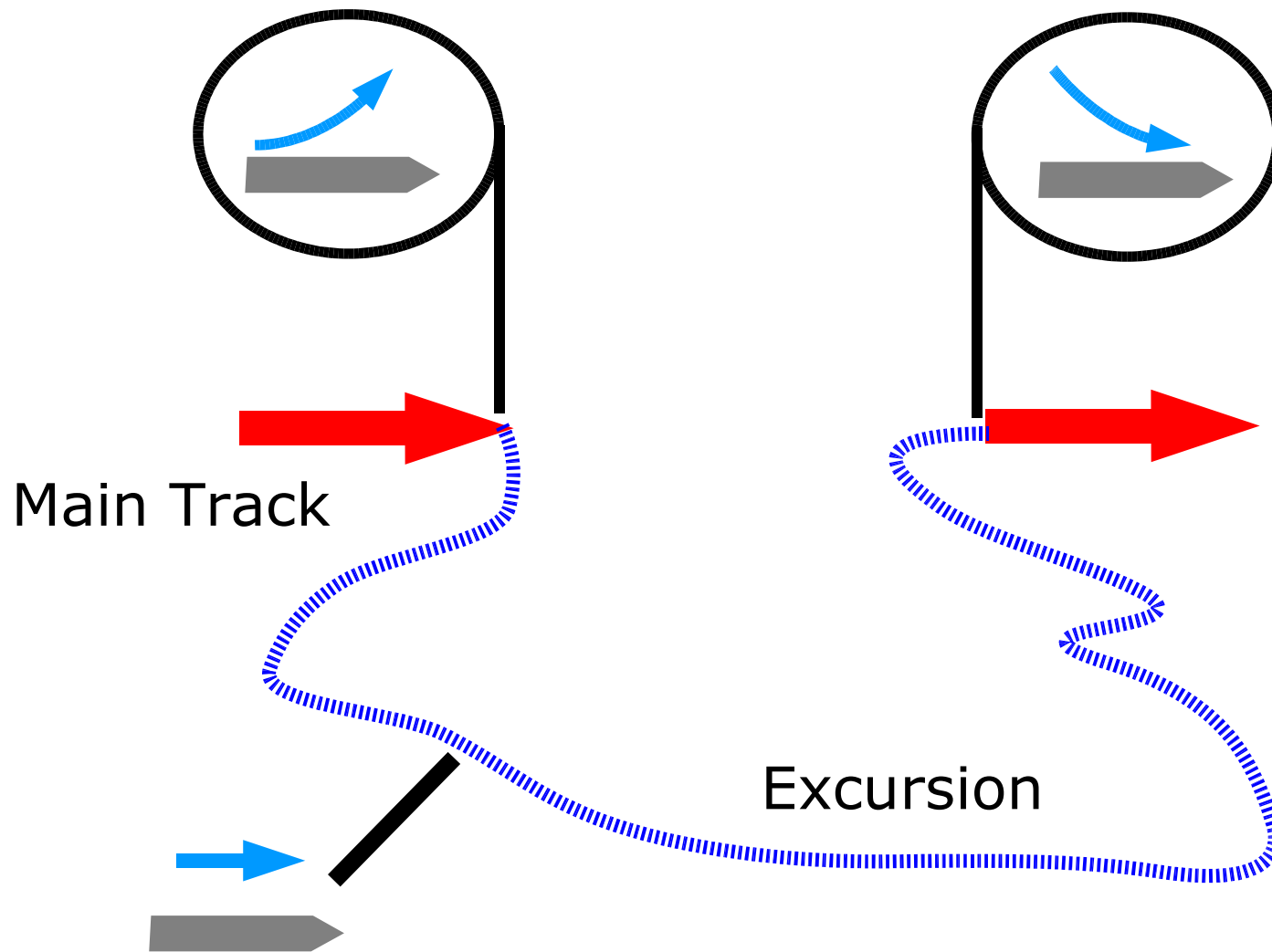


Martin Liendl
SWX Swiss Exchange

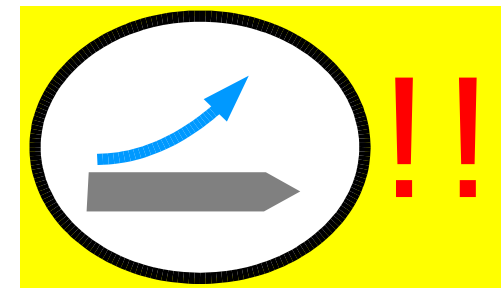
“Strategy”



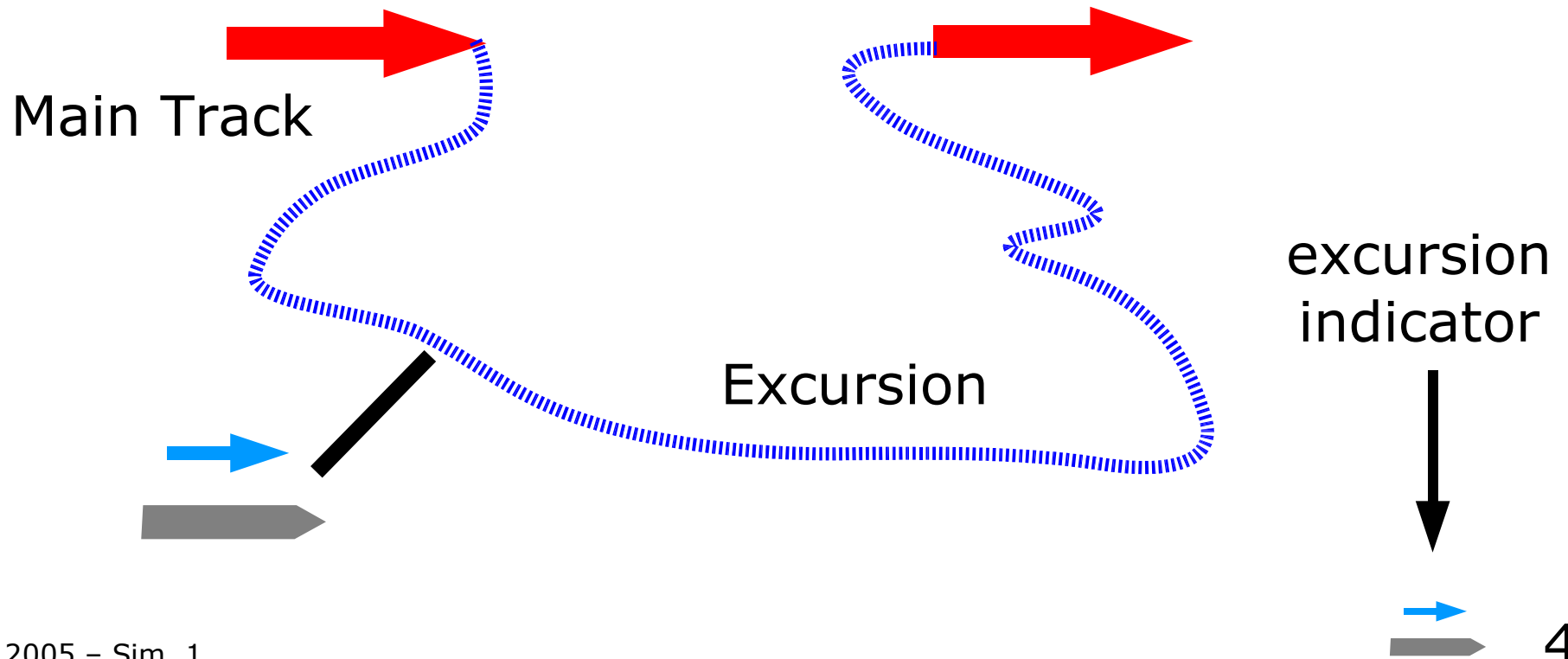
“Strategy”

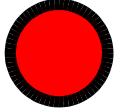
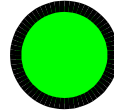


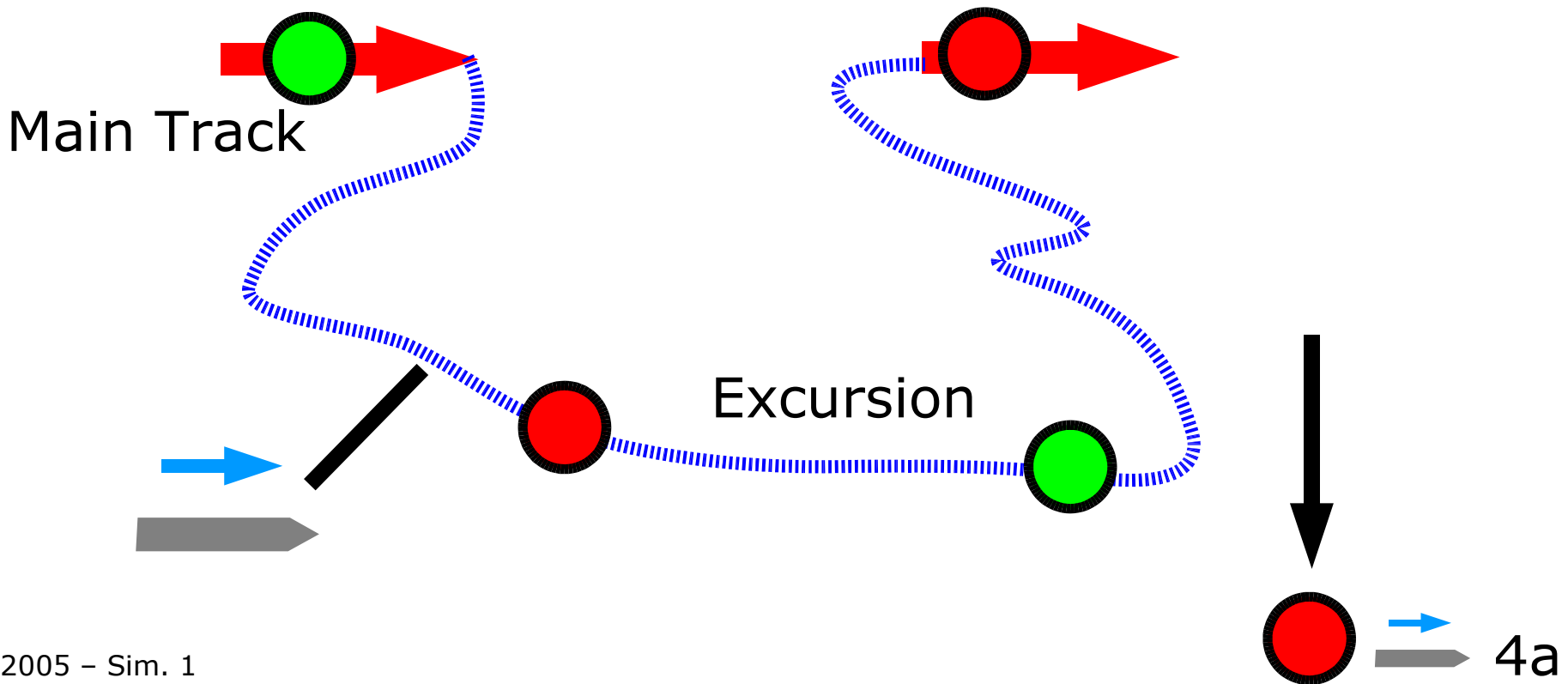
“Strategy”



Now we go on an excursion!



- Slides showing this symbol  are not contained in your handouts!
- Slides showing this symbol  have been modified from your handouts!
- You can download the updated version of the lectures from the CSC web.

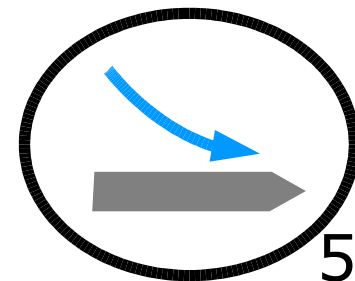


Overview of Lectures

- Experiment Simulation: What and Why
- Passage of Particles through Matter, physics models
- Monte Carlo Methods
- Introduction to GEANT4
- Geometry, Tracking
- Event loop, user hooks
- Introduction to Exercises



always a bit interrelated ...



Why & What

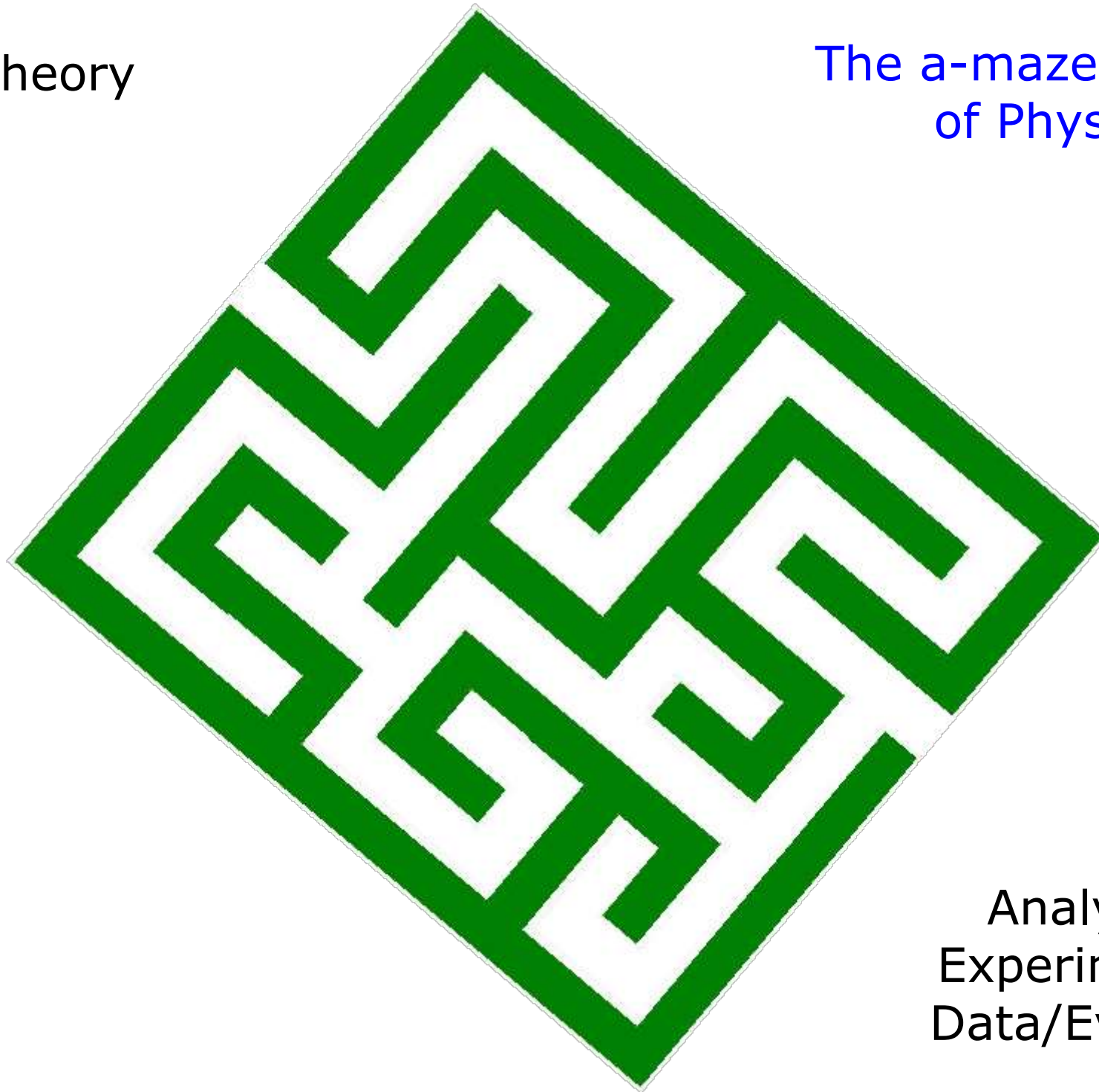
A (by far) non-exhaustive introduction ...

Some general ideas on how high energy physics experiments work in general

Will use (in parallel) a oversimplified
“Mickey Mouse”-model
to high-light some peculiar aspects

Theory

The a-maze-ing world
of Physics ..



Analyzed
Experimental
Data/Evidence

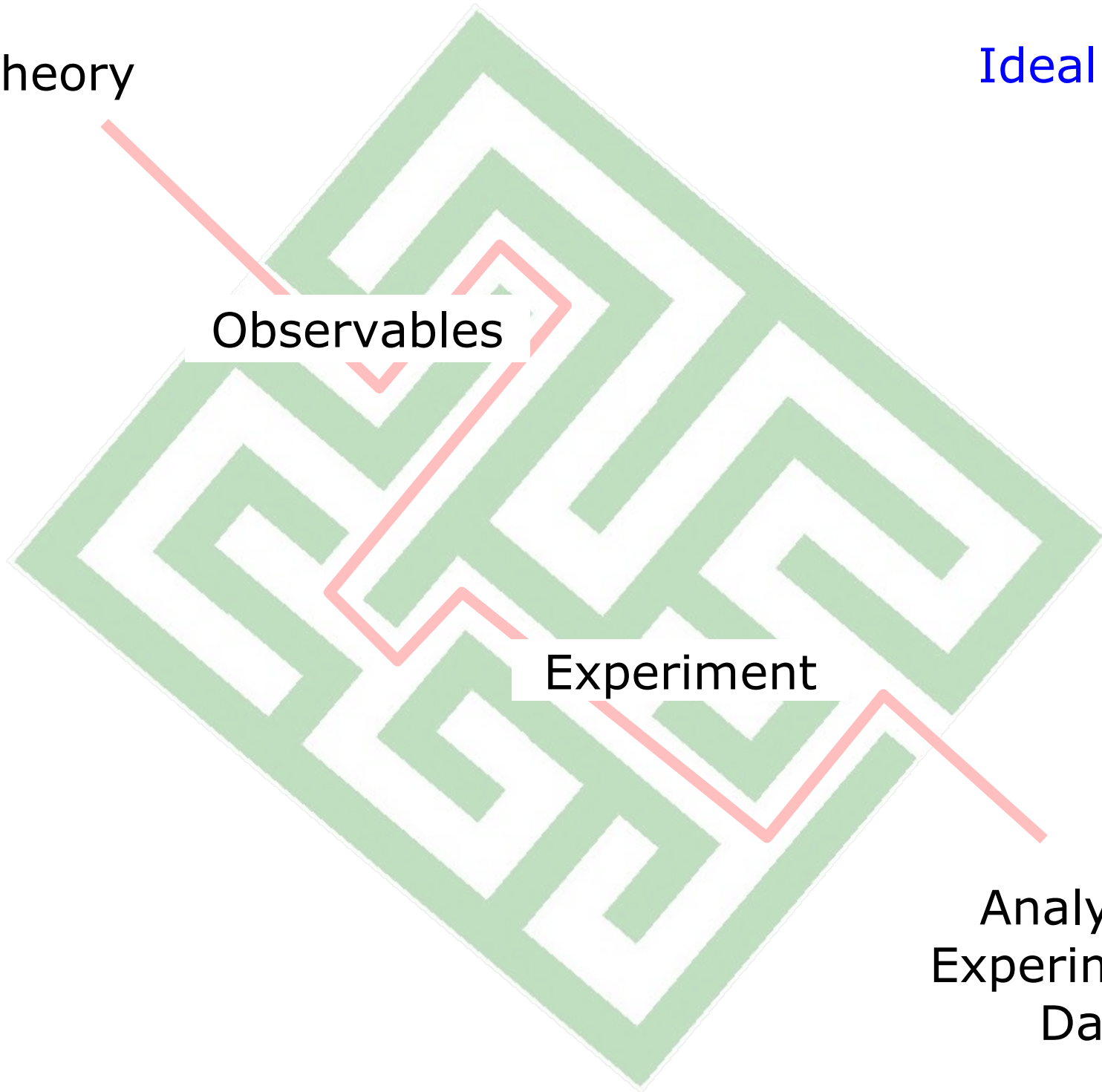
Theory

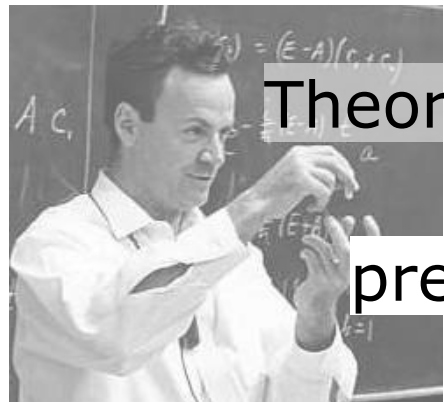
Ideally ...

Observables

Experiment

Analyzed
Experimental
Data





Theory

predicts

Observables

are measured

Experiment

outputs data

Analyzed
Experimental
Data

in HEP: orders of
magnitude everywhere!

OK, fine ...

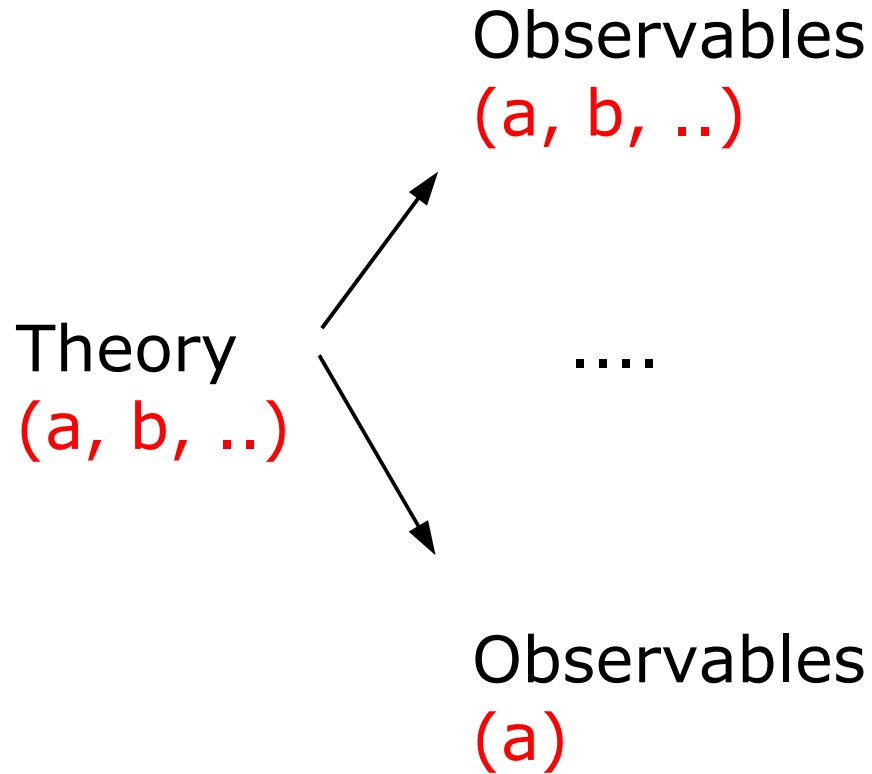
But why now **SIMULATION???**

Theory → Observables → Experiment → Analysis

Theory
(a, b, ..)

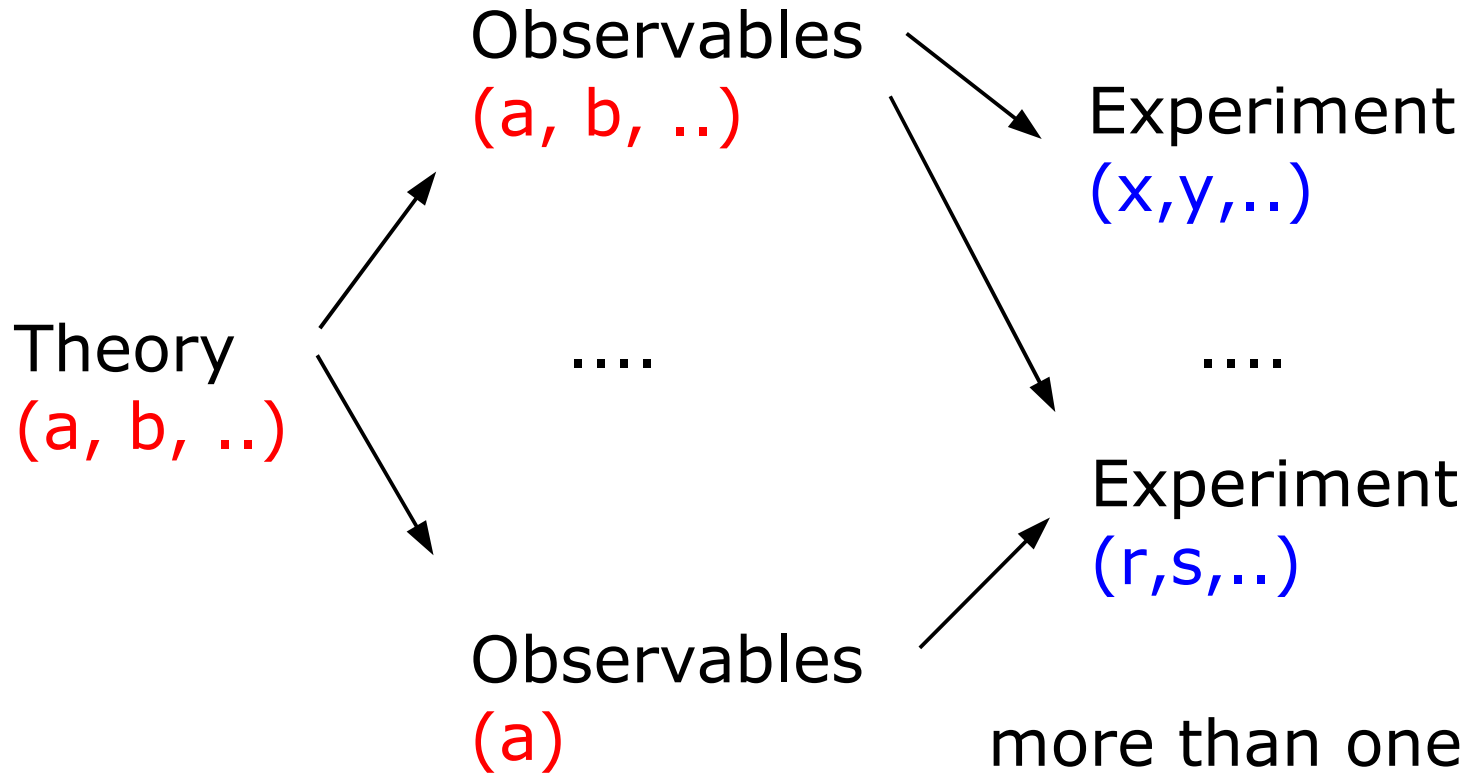
unknown values for
parameters in theory,
e.g. the mass of the Higgs

change in parameters,
change in prediction
of observables



unknown values for
parameters in theory,
e.g. the mass of the Higgs

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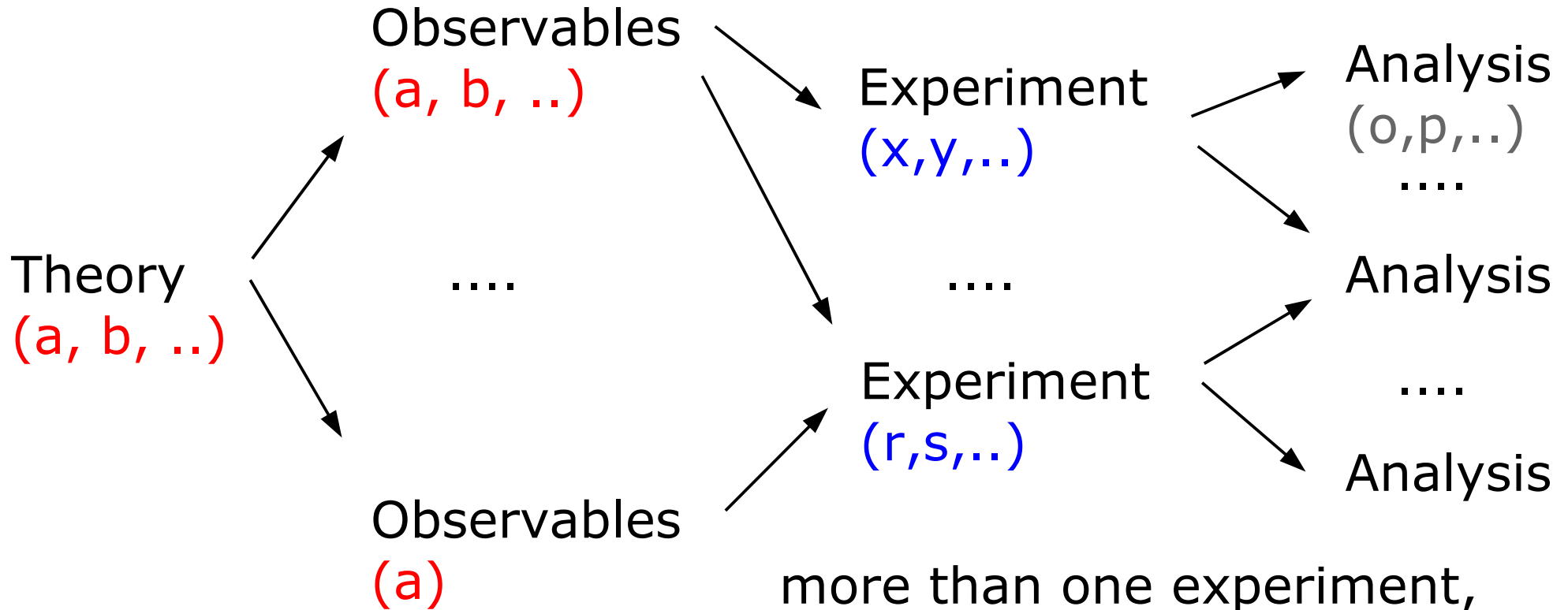


more than one experiment,
gains, gas pressures, voltages, ...
electronic noise, efficiency,
acceptance, dead channels,
machine conditions, ...

unknown values for
parameters in theory,
e.g. the mass of the Higgs

change in parameters,
change in prediction
of observables

choice of algorithm,
"cut" values, ...

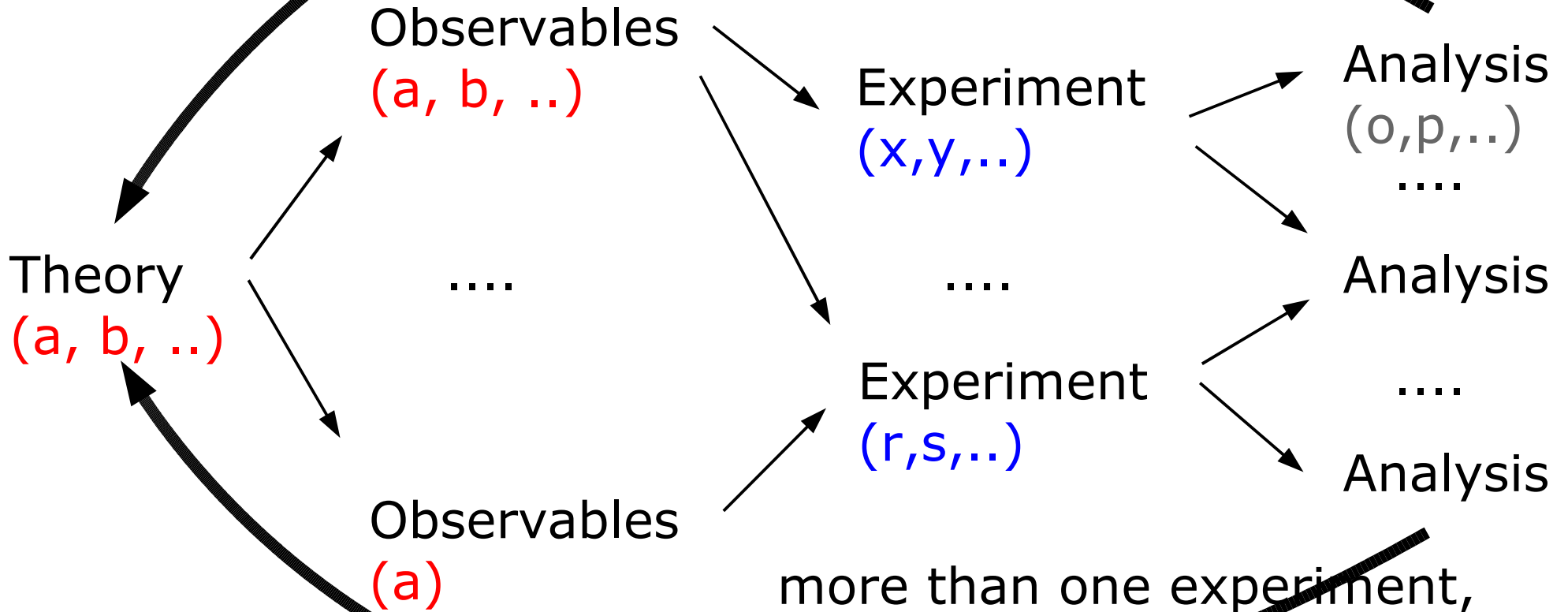


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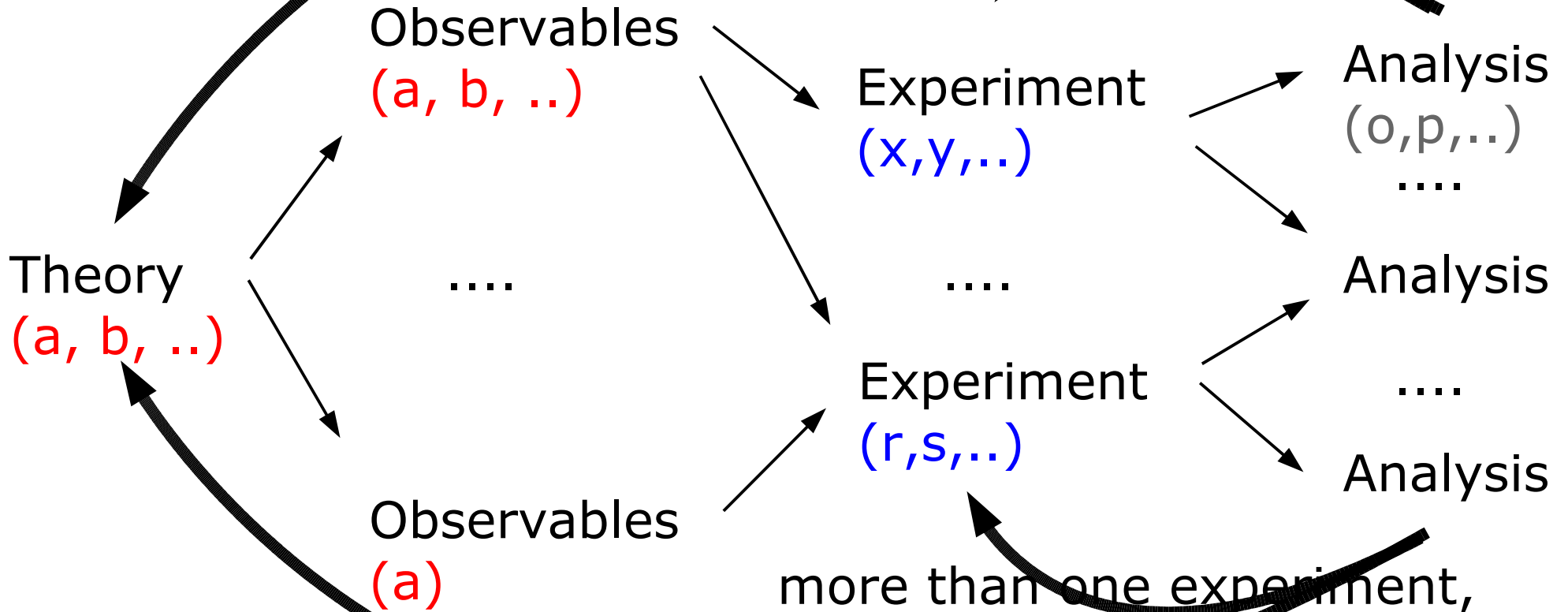


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change in parameters,
change in prediction

choice of algorithm,
"cut" values, ...

The need for simulation:

Because of the tremendous multiplicity of possible parameter constellations, it is impossible to design, operate, and "understand" today's HEP experiments without having corresponding simulation programs capable of "scanning" the allowed parameter ranges!

gains, gas pressures, voltages, ...
electronic noise, efficiency,
acceptance, dead channels,
machine conditions, ...

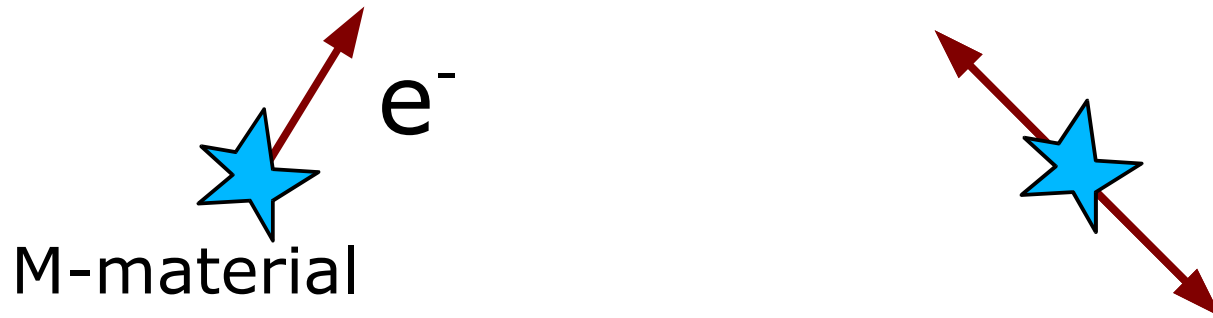
unknown values for
parameters in theory,
e.g. the mass of the Higgs

“understanding” your detector

(the – exaggerated simplified - Mickey Mouse case)

The Mickey Mouse Material

Somewhere in Disney World, Mickey finds ...
... the M-material emits spontaneously electrons
into a random direction (2D)


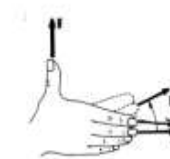



In Mickey's world everything is 2D, of course!

The Mickey Mouse Theory

M-Theory:

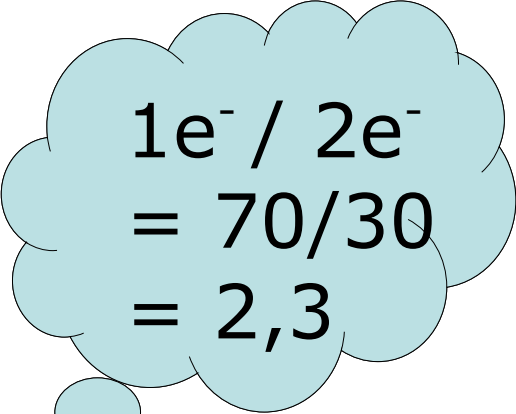
$\frac{1}{2}mv^2 = \frac{p^2}{2m}$ $W_{tot} = \Delta(K_{L, ...})$
 $k = 8.99 (10)^9 \left[\frac{Nm}{C^2} \right]$
 $\frac{1}{4\pi\epsilon_0} \frac{q_1q_2}{r^2}$ $\epsilon_0 = 8.85(10)^{-12} \left[\frac{C^2}{Nm^2} \right]$ $\epsilon_0 = 8.85(10)^{-12} \left[\frac{C^2}{Nm^2} \right]$
 $F = k \frac{q}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$ $V = k \frac{q}{r} = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$ $V = \frac{U}{q}$
 $\Delta A = \frac{q}{\epsilon_0}$ $Q = VC$ $C = \frac{A\epsilon_0}{d}$ $\sigma = \frac{Q}{A}$ $V = Ed$ $E = \frac{\sigma}{\epsilon_0}$ $U = \frac{QV}{2}$
 $\sum_{loop} V_j = 0$ $V = IR$ $P = IV = I^2 R = \frac{V^2}{R}$ $R_{eff} = R_1 + R_2$ $\frac{1}{R_{eff}} = \frac{1}{R_1} + \frac{1}{R_2}$
 $q v_{\perp} B = q v B \sin(\theta)$ $B = \frac{\mu}{r}$
 $\mathcal{B} = ILB \sin(\theta)$ μ

The Mickey Mouse Theory

M-Theory predicts:

- 1 cm² of M-material emits either one single or two electrons
- at a time
- into a random direction (2D)
- in case of two electrons, they are emitted into opposite direction


$$\begin{aligned} 1e^- / 2e^- \\ = 70/30 \\ = 2,3 \end{aligned}$$



70% of all events are $1e^-$
30% of all events are $2e^-$

on average: 1 event / sec per cm³

Theory predicts Observables





from

to



Mickey 's world

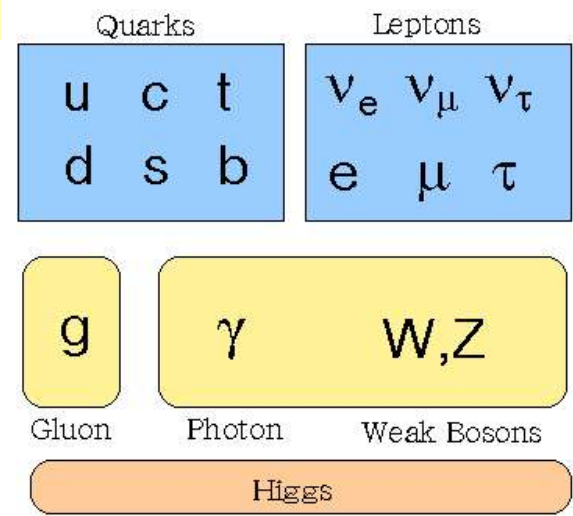
our world

Theory

Exercise 1.1.1.1a: Given locality, causality, Lorentz invariance, and known physical data since 1860, show that the Lagrangian describing all observed physical processes (sans gravity) can be written:

$$\begin{aligned}
 & -\frac{1}{2}\partial_\nu g_\mu^a \partial_\nu g_\mu^a - g_s f^{abc} \partial_\mu g_\nu^a g_\mu^b g_\nu^c - \frac{1}{4}g_s^2 f^{abc} f^{ade} g_\mu^b g_\nu^c g_\mu^d g_\nu^e + \\
 & \frac{1}{2}ig_s^2 (\bar{q}_i^\sigma \gamma^\mu q_j^\sigma) g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2} M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \right. \\
 & \left. \frac{2M}{g} H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2} \alpha_h - igc_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\mu^- W_\nu^+) - \mathcal{Z}^0 (W_\mu^+ \partial_\nu W_\mu^- - W_\mu^- \partial_\nu W_\mu^+) + \mathcal{Z}^0 (W_\mu^+ \partial_\nu W_\mu^- -
 \end{aligned}$$

..... (http://nuclear.ucdavis.edu/~tgutierr/files/stmL1.html)

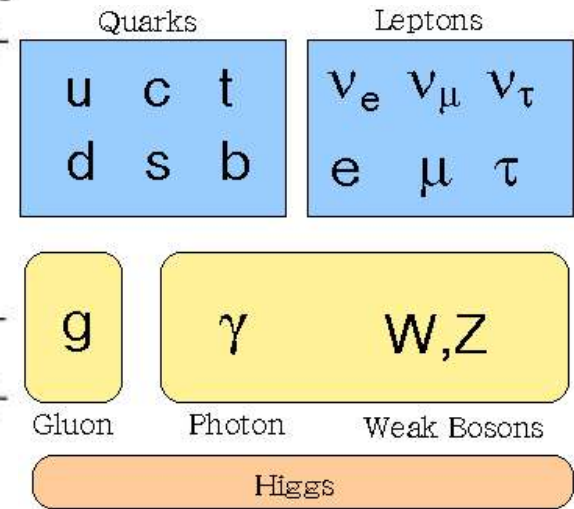


The Standard Model

Theory + Observables

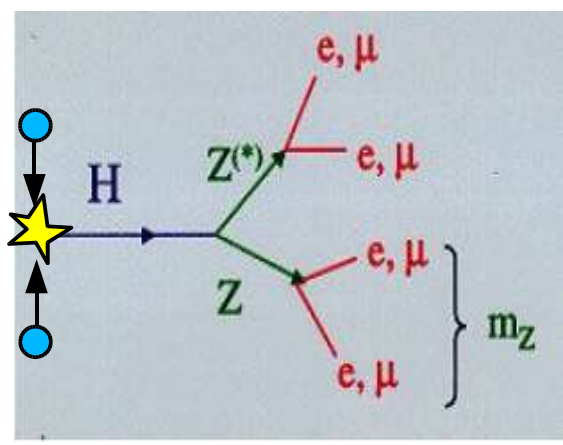
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$$\begin{aligned}
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 & \frac{1}{2}ig_s^2(\bar{q}_i^\sigma \gamma^\mu q_j^\sigma)g_\mu^a + \bar{G}^a \partial^2 G^a + g_s f^{abc} \partial_\mu \bar{G}^a G^b g_\mu^c - \partial_\nu W_\mu^+ \partial_\nu W_\mu^- - \\
 & M^2 W_\mu^+ W_\mu^- - \frac{1}{2}\partial_\nu Z_\mu^0 \partial_\nu Z_\mu^0 - \frac{1}{2c_w^2}M^2 Z_\mu^0 Z_\mu^0 - \frac{1}{2}\partial_\mu A_\nu \partial_\mu A_\nu - \frac{1}{2}\partial_\mu H \partial_\mu H - \\
 & \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^- - M^2 \phi^+ \phi^- - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2}M\phi^0 \phi^0 - \beta_h \left[\frac{2M^2}{g^2} + \right. \\
 & \left. \frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) \right] + \frac{2M^4}{g^2}\alpha_h - igc_w [\partial_\nu Z_\mu^0 (W_\mu^+ W_\nu^- - \\
 & W_\mu^- W_\nu^+) - Z^0 (W_\mu^+ \partial_\nu W_\nu^- - W_\mu^- \partial_\nu W_\nu^+) + Z^0 (W_\mu^+ \partial_\nu W_\nu^- -
 \end{aligned}$$



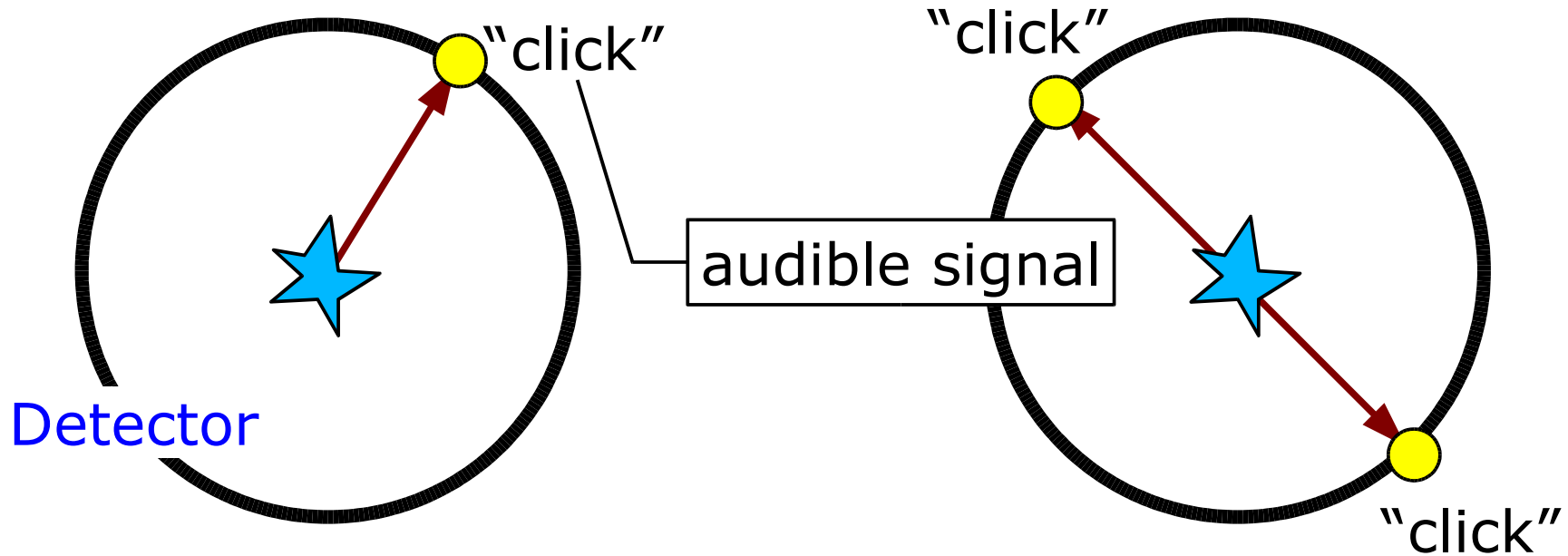
..... (http://nuclear.ucdavis.edu/~tgutierr/files/stmL1.html)

Observables: have a proton-proton collisions to make quarks interact. Sometimes, a Higgs particle will be produced, which decays in Zs, which decay in a pair of leptons ...



The leptons are the observables, because they can be detected by a particle detector, and they live long enough to be detected.

Mickey's "Gedankenexperiment"

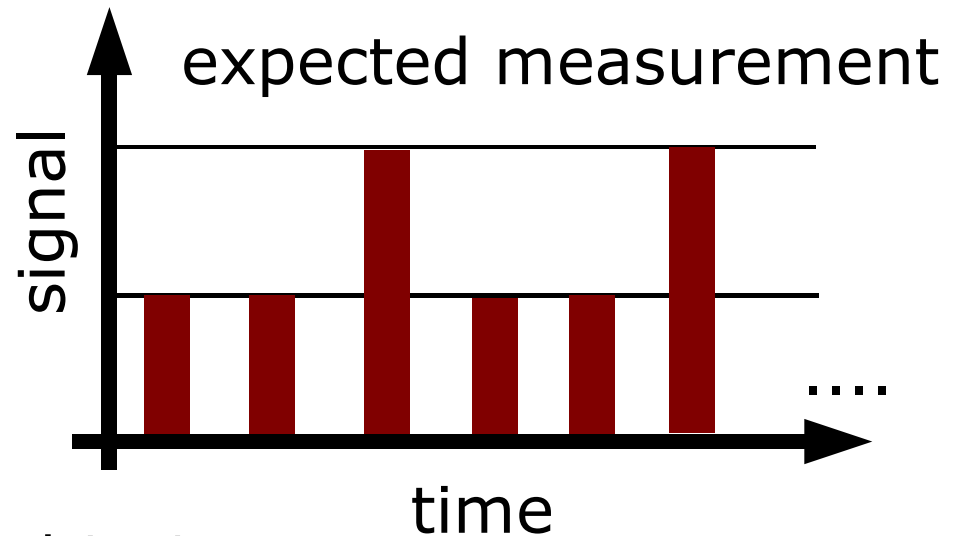


M-Theory says:

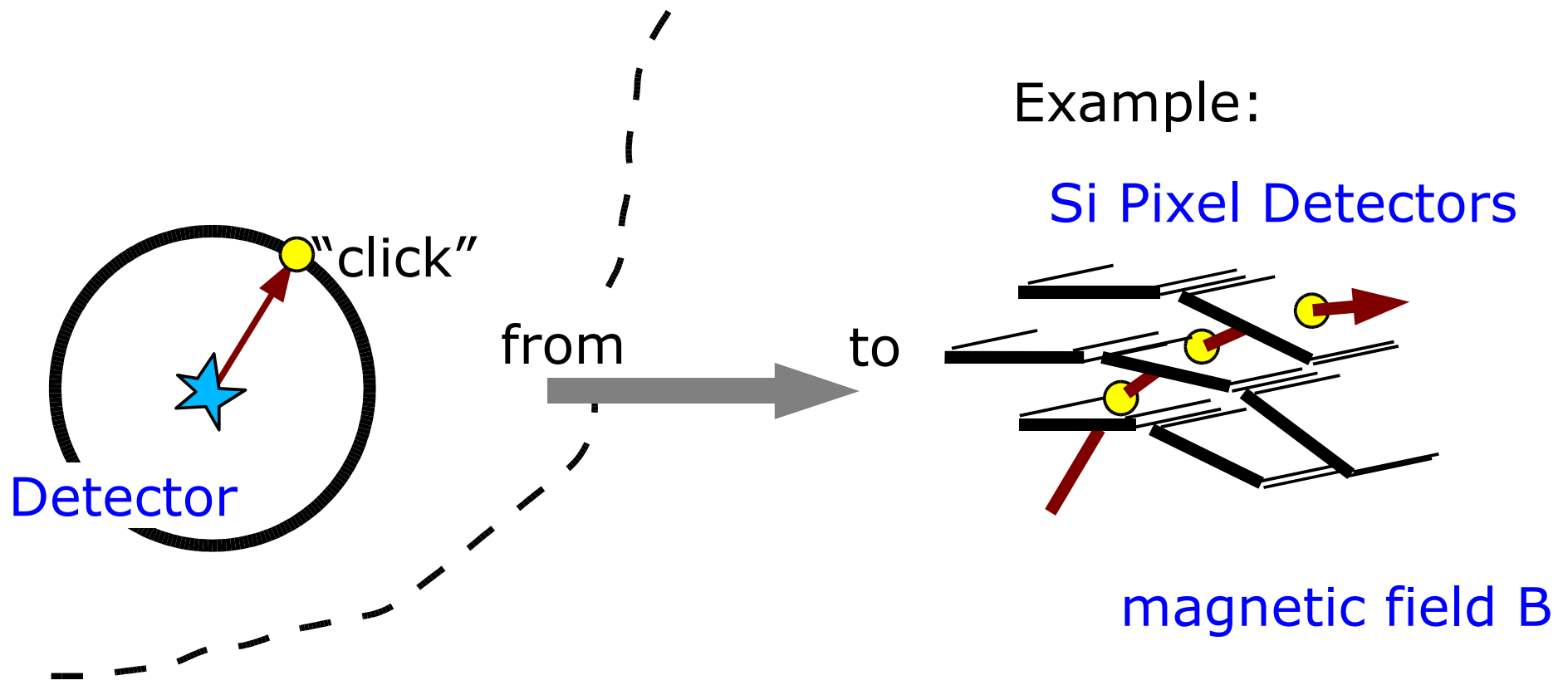
$$1 e^- / 2 e^- = 2,3$$

If Experiment measures:

$$1 \text{ click} / 2 \text{ clicks} = 2,3$$



then theory and experiment are consistent.



- ... - muon interaction with matter:
 - . ionization
 - . bremsstrahlung
 - . Coulomb scattering
- muon interaction with B-field
 - . curved flight path

Expected measurement: points on a particle trajectory

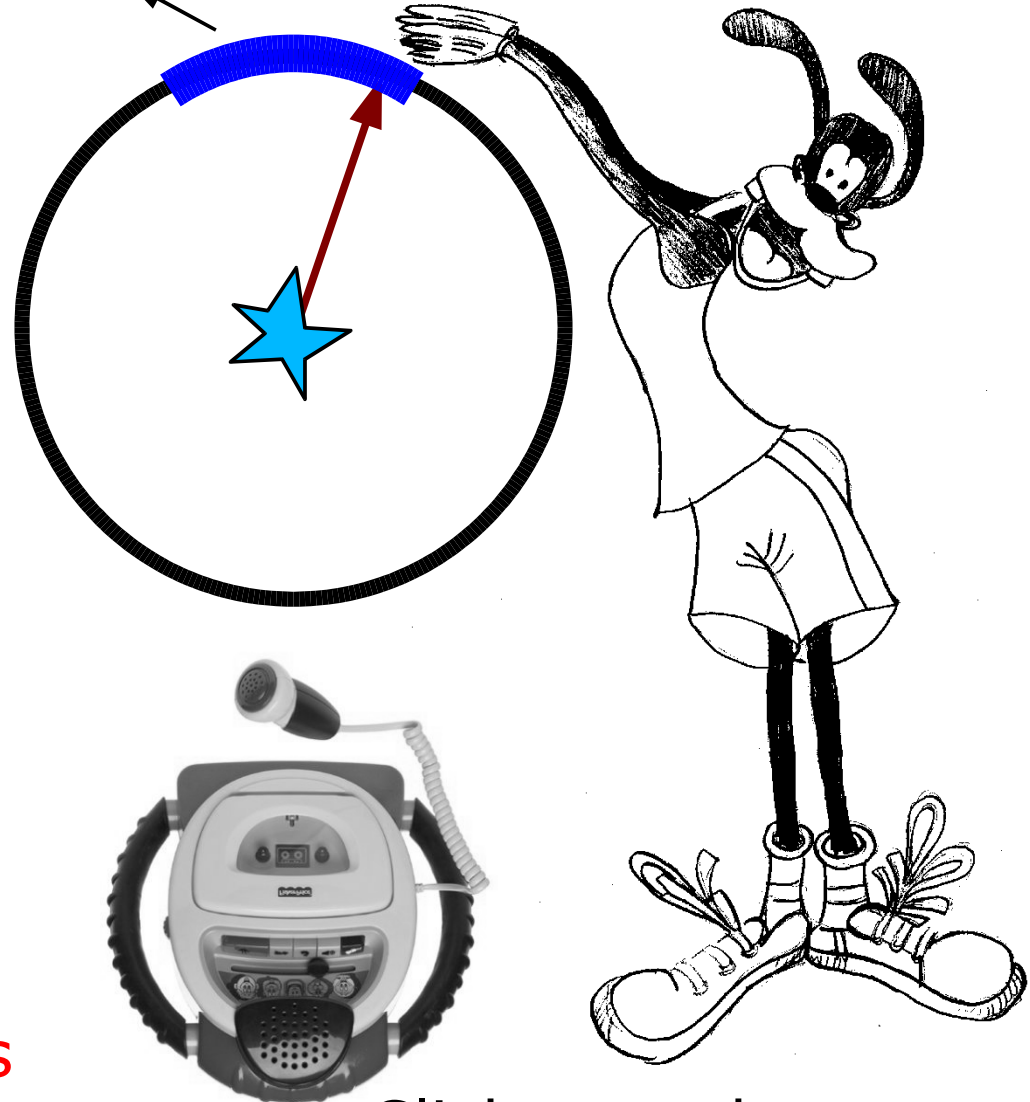
The Mickey Mouse Experiment

In Disney World,
Goofy builds
the detector.

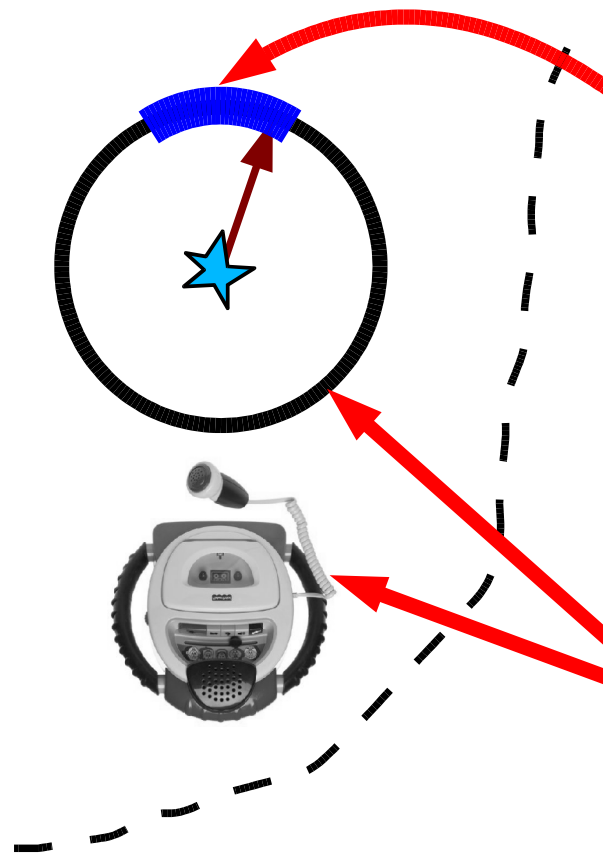
He has to use
a **cooling pipe**
taking 20%
of the surface
of the detector's
sensitive area

**Technical Know How
and How To for
measuring observables**

no "click" here

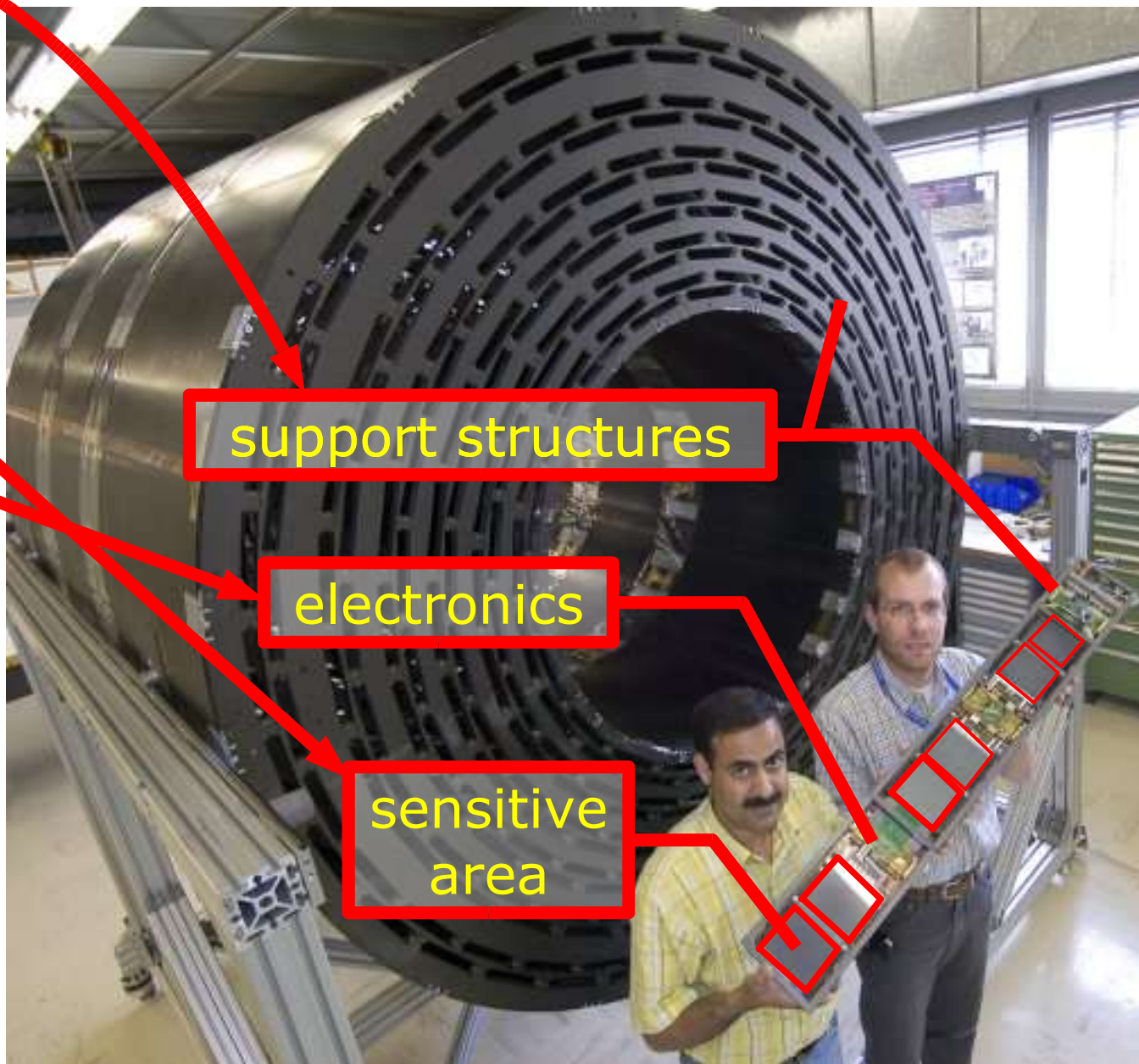


Click recorder

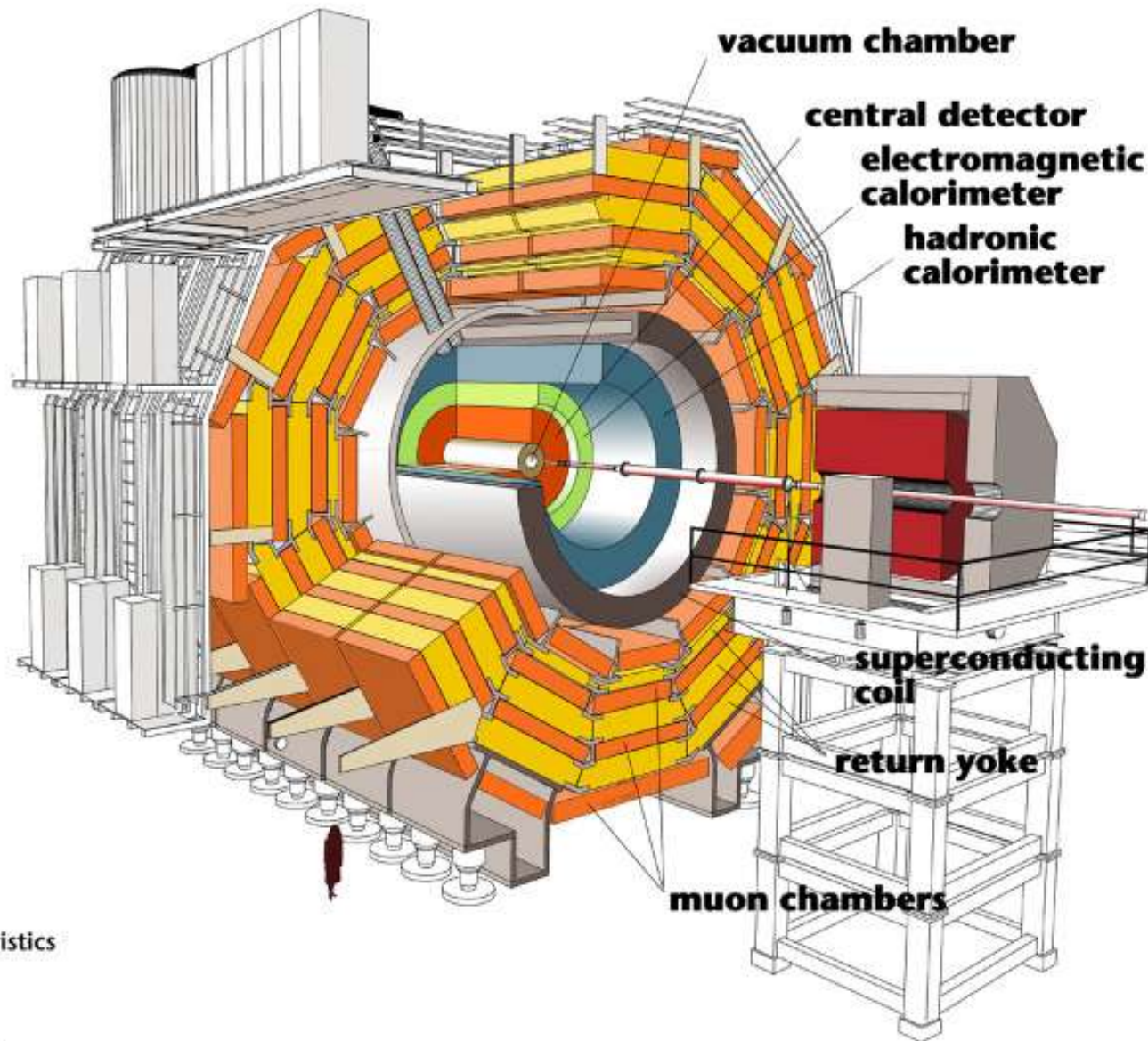


Not shown:
trigger electronics,
data storage, ...

And: it's "only" a
part of a sub-detector!



We need this:

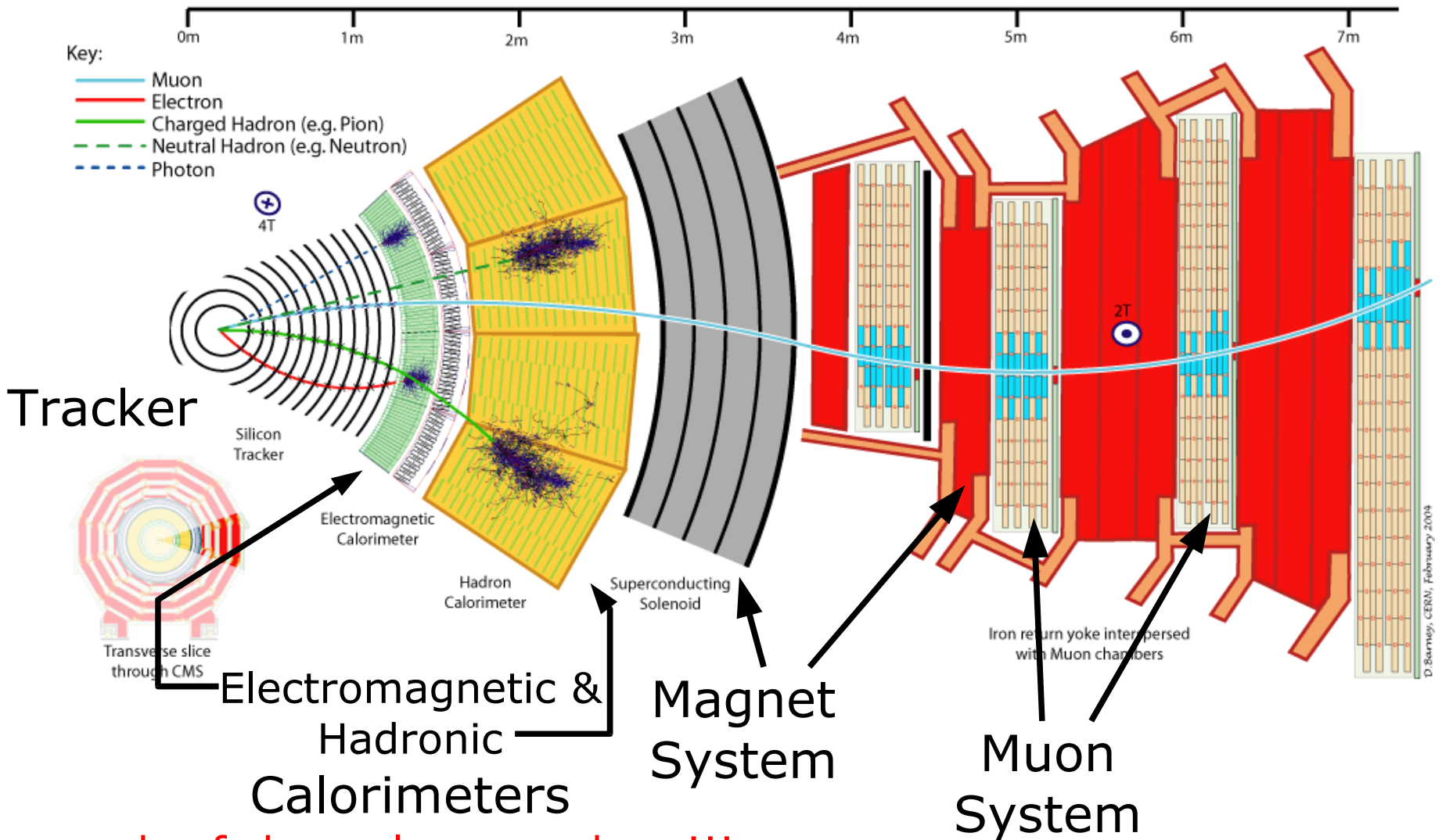


Detector characteristics

Width: 22m
Diameter: 15m
Weight: 14'500t

We need this:

Onion shell design exploiting the physics processes of (“long living”) particles traversing bulk matter

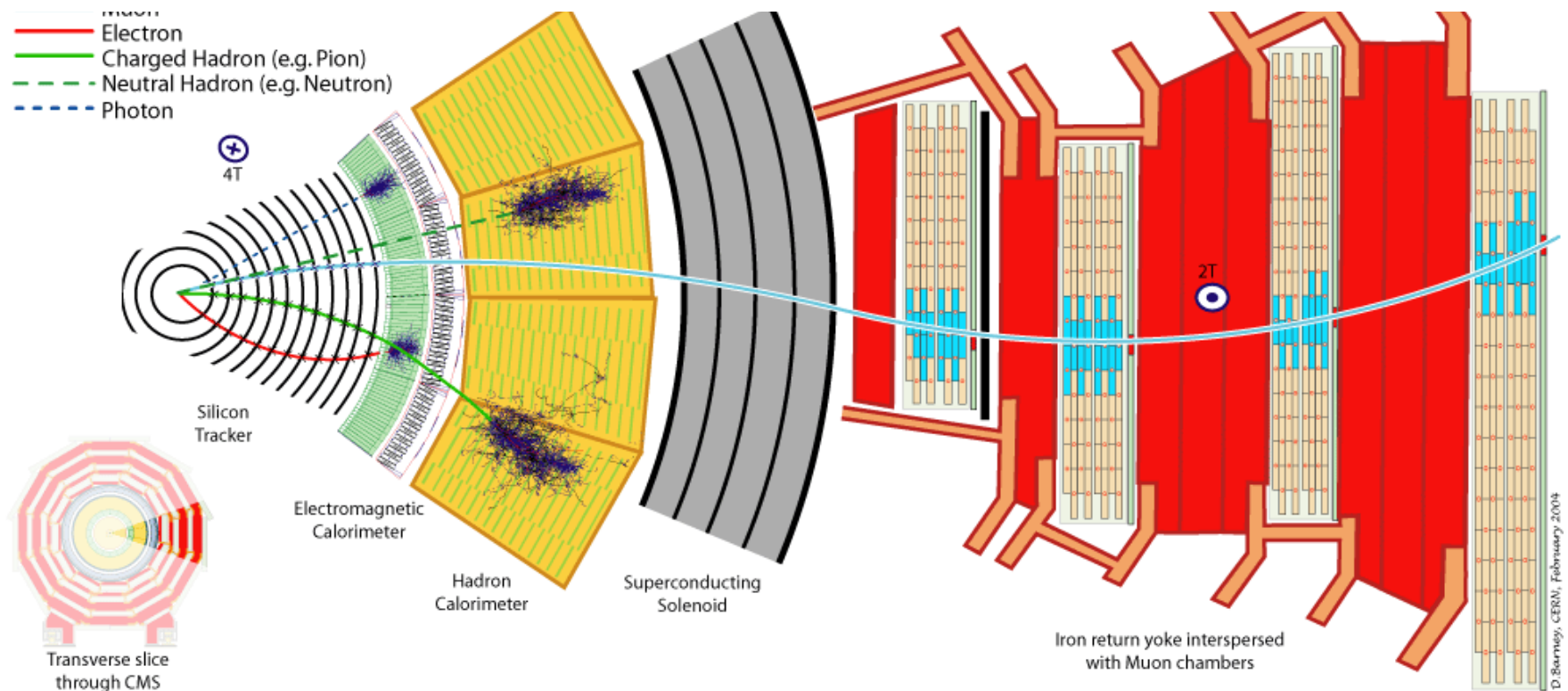


Thousands of channels everywhere!!!
Complex geometry

This lectures are mainly about how to simulate particles interacting with and traversing bulk materials:

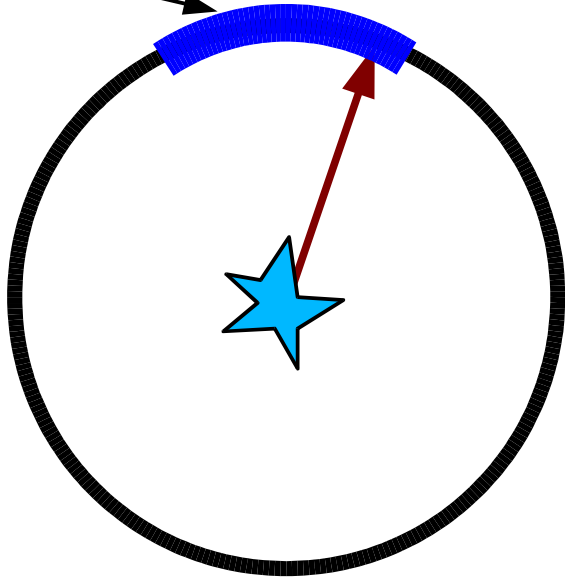
- how to describe a detector made of bulk materials
- how to track single particles through it
- how to model the physics of their interactions

using the simulation toolkit GEANT4 as an example



Doing the experiment

non sensitive
cooling pipe no "click" here



Now, Mickey measures:

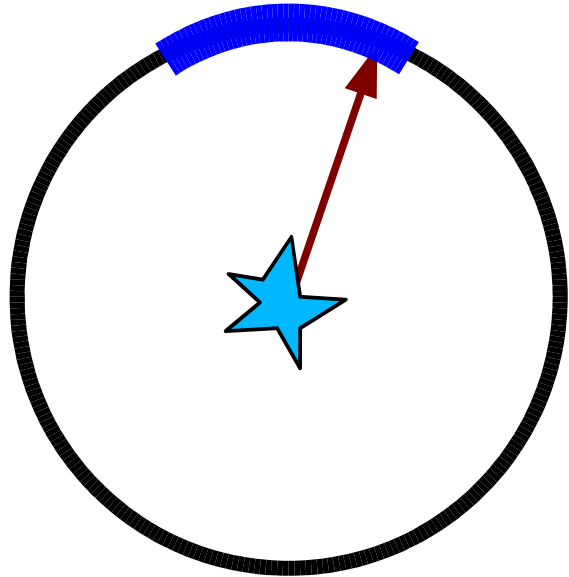
$$1 \text{ click} / 2 \text{ clicks} = 2,6$$

$$\text{Theory: } 1 e^- / 2 e^- = 2,3$$

Is the experiment still consistent with the theory?
Or does the experiment prove the theory wrong?

The Mickey Mouse Analysis

Thought:



We loose 20% of the sensitive area, thus we measure 20% less events (20% less 1 clicks, 20% less 2 clicks)

but then the ratio between 1 and 2 click counts should be the same!

=> the experiment indicates that the theory is not correct!

Theory:

$$1 e^- / 2 e^- = 2,3$$

Experiment:

$$1 \text{ click} / 2 \text{ clicks} = 2,6$$

and thus:

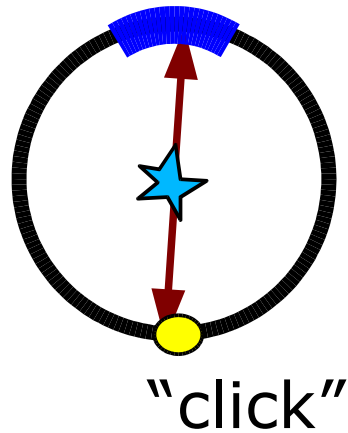
$$1 e^- / 2 e^- = 2,6$$

Understand
and analyze the
measurements

Some 2 e⁻ events are counted as 1 e⁻ events!!

=> 20% of the 1e⁻ events are lost

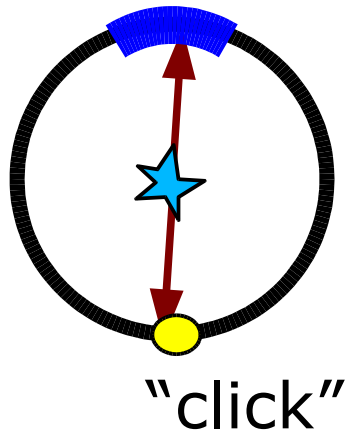
=> 20% of the 2e⁻ events are counted as 1e⁻



ATTENTION!

Understand
and analyze the
measurements

Some 2 e⁻ events are counted as 1 e⁻ events!!



- => 20% of the 1e⁻ events are lost
- => 20% of the 2e⁻ events are counted as 1e⁻

Assuming the M-Theory:

We have N events per hour, then
0.7N are 1e⁻ events
0.3N are 2e⁻ events

Detector sees:

0.7N - 20% 1e⁻ → 0.56N single clicks (20% less single clicks)
0.3N - 20% 2e⁻ → 0.24N double clicks (20% less double clicks)
→ (0.3 - 0.24)N = 0.06N doubles counted as singles!

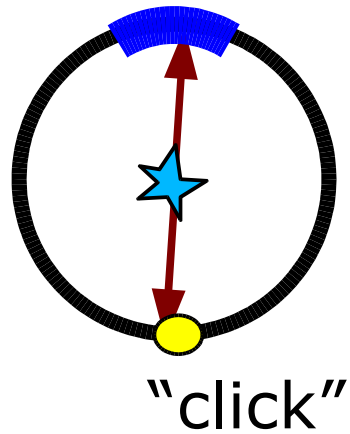
=> additional 0,06N single clicks

single clicks: 0,56N + 0,06N = 0,62N

double clicks: 0,24N

$$1 \text{ click} / 2 \text{ clicks} = 62/24 = 2,6$$

Some 2 e⁻ events are counted as 1 e⁻ events!!



=> 20% of the 1e⁻ events are lost

=> 20% of the 2e⁻ events are counted as 1e⁻

Assuming the M-Theory:

$$1 e^- / 2 e^- = 2,3$$

AND understanding the detector & the measurement, the measured ratio must be bigger to be consistent with the theory:

$$\begin{aligned} 1 \text{ click} / 2 \text{ clicks} &= 62/24 \\ &= 2,6 \end{aligned}$$



Efficiency/Acceptance, Background

Mickey needed to know the **efficiency/acceptance and background** of his detector to interpret the result correctly.

For the same type of event, the **acceptance** is defined as:

$$\langle N_{\text{measured}} \rangle = a \cdot \langle N_{\text{occurred}} \rangle + \langle N_{\text{bckgrd}} \rangle$$

Diagram illustrating the definition of acceptance:

- $\langle N_{\text{measured}} \rangle$: average measured events looking like type X
- a : acceptance
- $\langle N_{\text{occurred}} \rangle$: average of real events of type X
- $\langle N_{\text{bckgrd}} \rangle$: Background looking like type X

Intuitively, for Mickey's experiment:

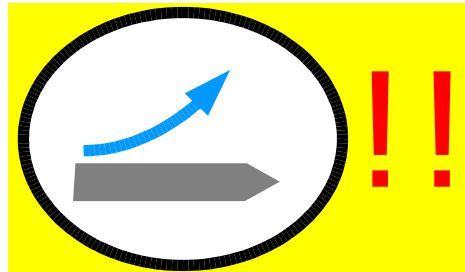
acceptance for measuring 1 e^- events = 0.8

acceptance for measuring 2 e^- events = 0.8

Efficiency & Acceptance

If we look only on one particular event, we define:

Detection Efficiency $\varepsilon(x)$:= probability of an event to be detected if it has taken place



$x = (x_1, x_2, \dots)$... physical variables describing the event
(momenta of particles, position of vertices, ...)

Efficiency & Acceptance

Detection Efficiency $\varepsilon(\mathbf{x})$:= probability of an event to be detected if it has taken place

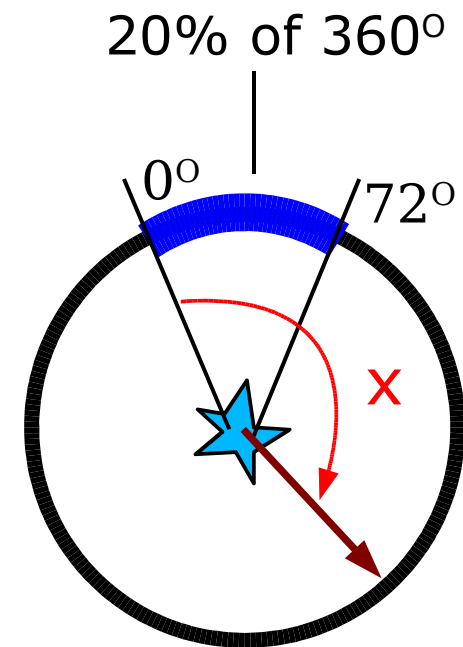
In Mickey's experiment for $1e^-$ events:

\mathbf{x} ... angle of emission

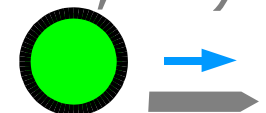
$\varepsilon(\mathbf{x}) = 1$, for \mathbf{x} within $72^\circ \rightarrow 360^\circ$

$\varepsilon(\mathbf{x}) = 0$, for \mathbf{x} within $0^\circ \rightarrow 72^\circ$

Special case of **geometrical efficiency!**



$\mathbf{x} = (x_1, x_2, ..)$... physical variables describing the event
(momenta of particles, position of vertices, ...)



Efficiency & Acceptance

In Mickey's world, things were simple ...

Detection Efficiency $\varepsilon(\mathbf{x})$:= probability of an event to be detected if it has taken place

dead time of channels | triggering

$$\varepsilon(\mathbf{x}) \sim \varepsilon_1(\mathbf{x}) \cdot \varepsilon_2(\mathbf{x}) \cdot \varepsilon_3(\mathbf{x}) \dots \cdot \varepsilon_g(\mathbf{x})$$

geometrical efficiency

$\varepsilon_g(\mathbf{x}) = 1 \leftrightarrow$ particle hit the detector (geometrically)

$\varepsilon_g(\mathbf{x}) = 0 \leftrightarrow$ particle missed the detector

$\mathbf{x} = (x_1, x_2, \dots)$... physical variables describing the event
(momenta of particles, position of vertices, ...)

Efficiency & Acceptance

The average (expectation value) of $\varepsilon(x)$ is then the acceptance:

Detection Efficiency $\varepsilon(x)$:= probability of an event to be detected if it has taken place

Acceptance a := average efficiency = $\langle \varepsilon \rangle$

$$= \int \varepsilon(x) f(x) dx$$

$f(x)$... probability density of event x (**quantum theories only give you probabilities!!!**)

$x = (x_1, x_2, \dots)$... physical variables describing the event (momenta of particles, position of vertices, ...)

Efficiency & Acceptance

Prediction of quantum theory

$$\int_{x_1}^{x_2} f(x) dx$$

Probability of x being between x_1 and x_2

(normalization value) of $\epsilon(x)$ is then the

probability to detect an occurred event having occurred in any of its possible states

to be placed

$a :=$ average efficiency = $\langle \epsilon \rangle$

$$a = \int \epsilon(x) f(x) dx$$

$f(x)$... probability density of event x (**quantum theories only give you probabilities!!!**)

$x = (x_1, x_2, \dots)$... physical variables describing the event (momenta of particles, position of vertices, ...)

Detection Efficiency $\varepsilon(\mathbf{x})$:= probability of an event to be detected if it has taken place

Acceptance a := average efficiency = $\langle \varepsilon \rangle$

$$a = \int \varepsilon(\mathbf{x}) f(\mathbf{x}) d\mathbf{x}$$

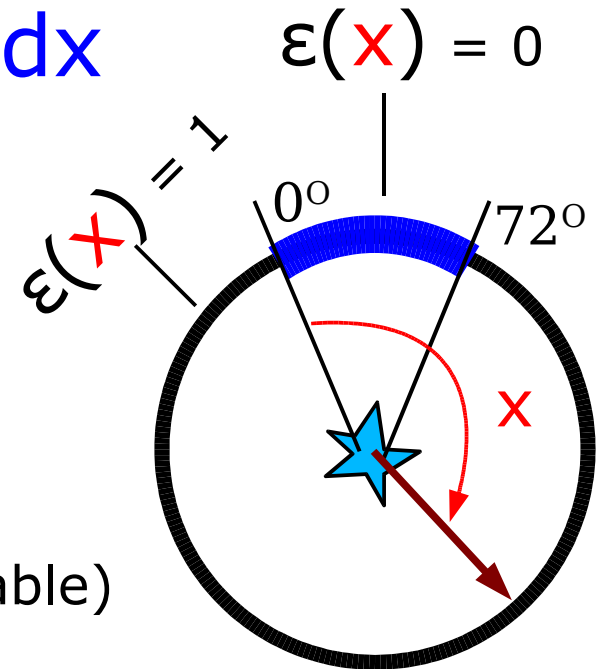
In Mickey's experiment for $1e^-$ events:

\mathbf{x} ... angle of emission

$\varepsilon(\mathbf{x}) = 1$, for \mathbf{x} within $72^\circ \rightarrow 360^\circ$

$\varepsilon(\mathbf{x}) = 0$, for \mathbf{x} within $0^\circ \rightarrow 72^\circ$

$f(\mathbf{x}) = 1/360^\circ$ (every direction equally probable)



$$a = \int f(\mathbf{x}) \varepsilon(\mathbf{x}) d\mathbf{x} = 1/360^\circ \left(\int_{72^\circ}^{360^\circ} 1 d\mathbf{x} + \int_{0^\circ}^{72^\circ} 0 d\mathbf{x} \right) = 288/360 = \underline{\underline{0.8}}$$

Efficiency & Acceptance

Mickey needed to know the efficiency and acceptance of his detector to interpret the measurement result correctly, and correct it by accounting for background events!

Detection Efficiency ε := probability of an event to be detected if it has taken place

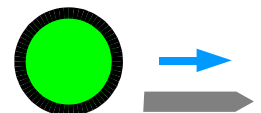
Acceptance a := average efficiency = $\langle \varepsilon \rangle$

$$\langle N_{\text{measured}} \rangle = a \langle N_{\text{occured}} \rangle \text{ for the same type of event!}$$

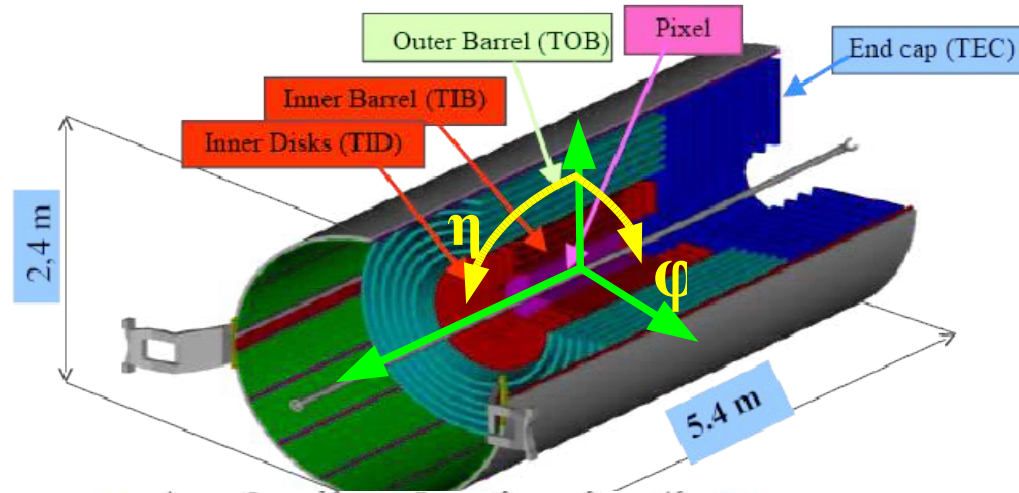
special case: geometrical acceptance

Mickey's experiment:

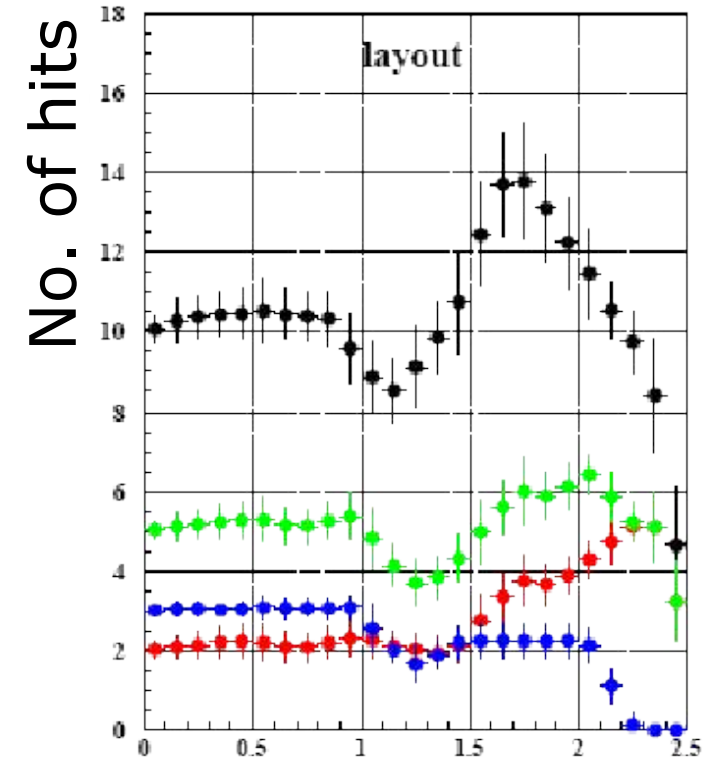
$a = 0,8$ (100% - 20% non sensitive detector)



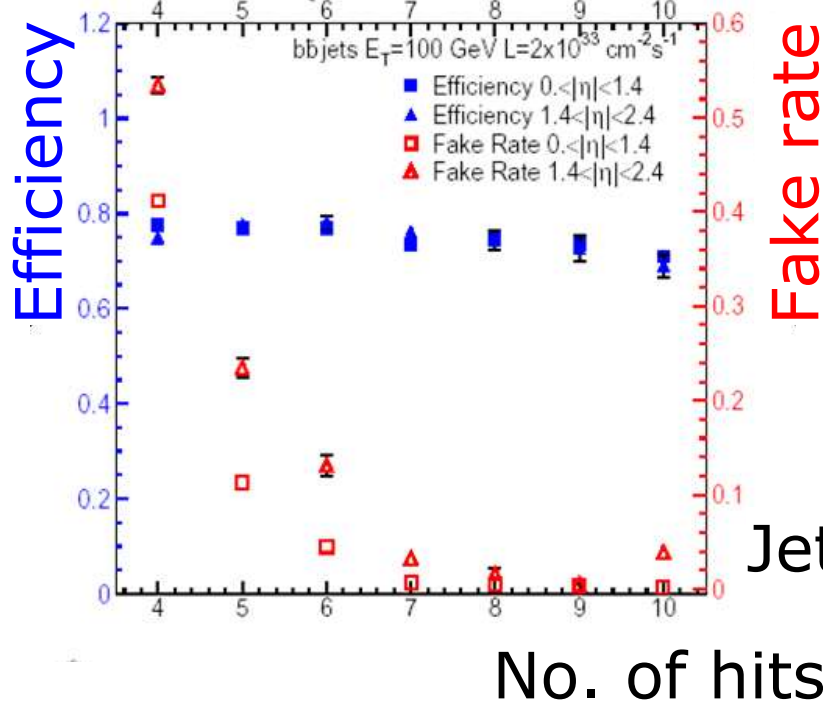
Example: CMS tracker average hits around ϕ by simulation



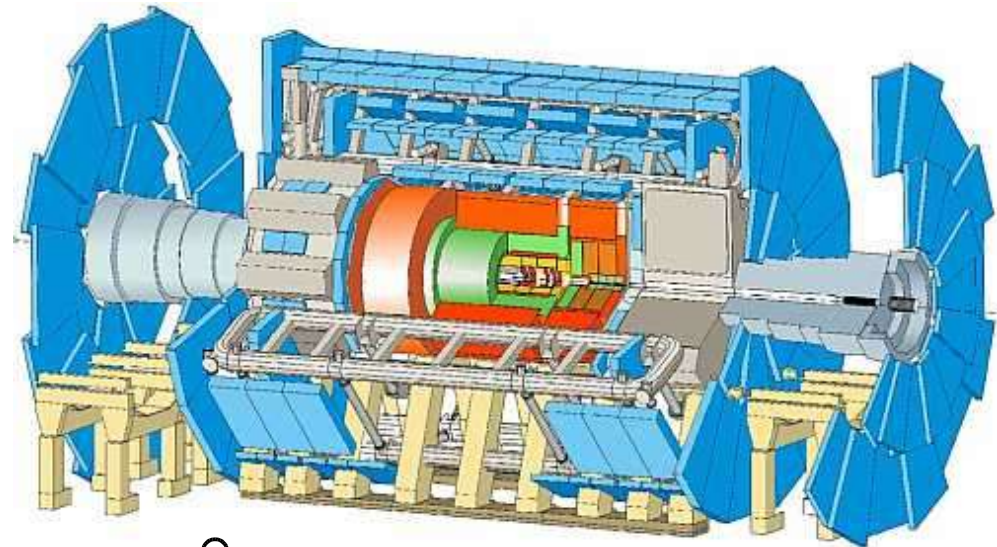
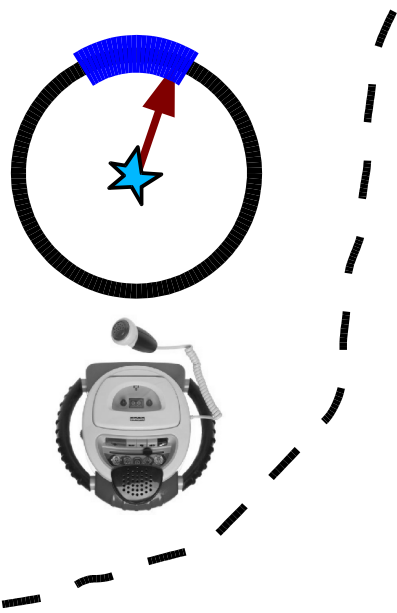
Number of SST hits by tracks:



Black: Total number of hits
 Green: double-sided hits
 Red: double-sided hits in thin detectors
 Blue: double sided hits in thick detectors.



Jet reconstruction efficiency



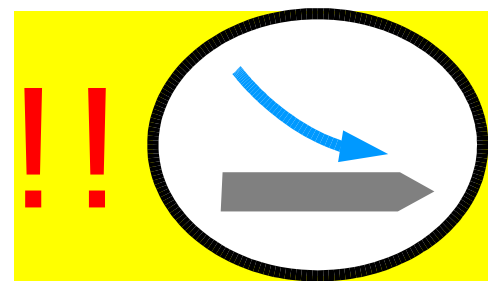
♀

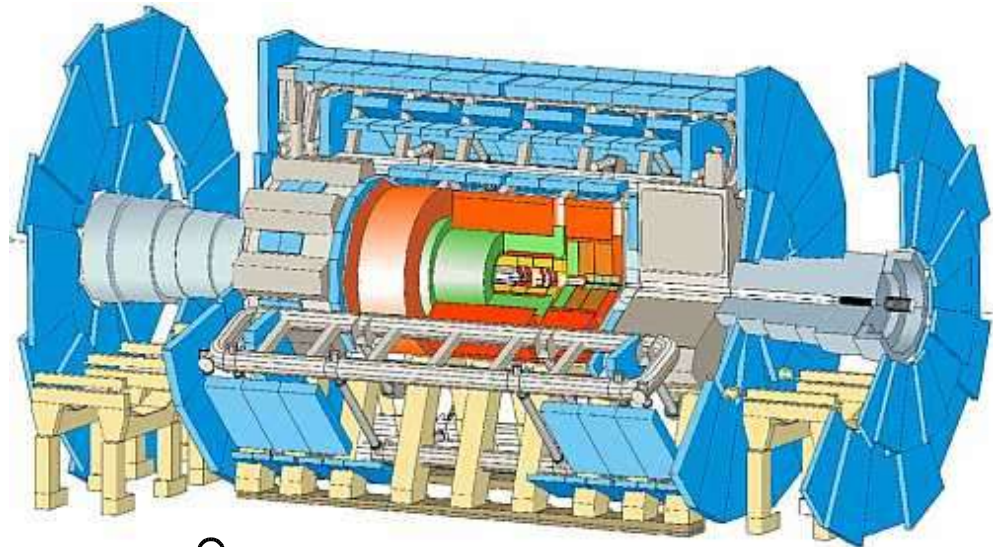
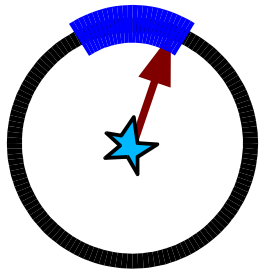
Generally, efficiency depends on many things:

- money
- geometry
- choice of sub-detectors (physical properties, deterioration, ..)
- event type
- trigger efficiencies
- reconstruction & analysis algorithms / SW & computing

How can we design & built a detector "efficiently" enough to measure what we want to measure?

=> simulation studies contribute significantly to the taken decisions





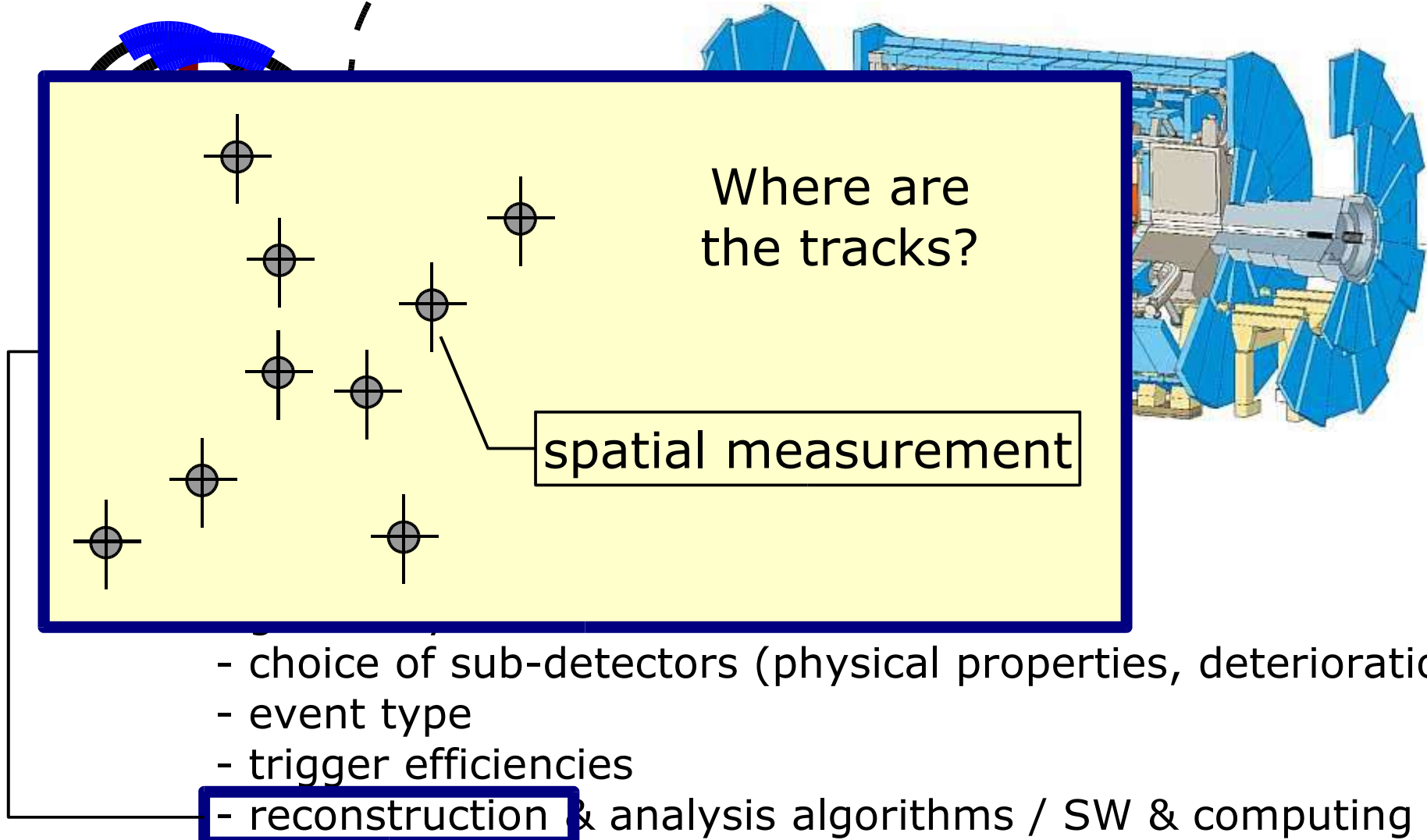
⊗

dead time of electronics, selection algorithms (LHC: 10^9 to 100 Hz!!) depends on many things:

- choice of sub-detectors (physical properties, deterioration, ..)
- event type
- trigger efficiencies
- reconstruction & analysis algorithms / SW & computing

How can we design & built a detector "efficiently" enough to measure what we want to measure?

=> simulation studies contribute significantly to the taken decisions



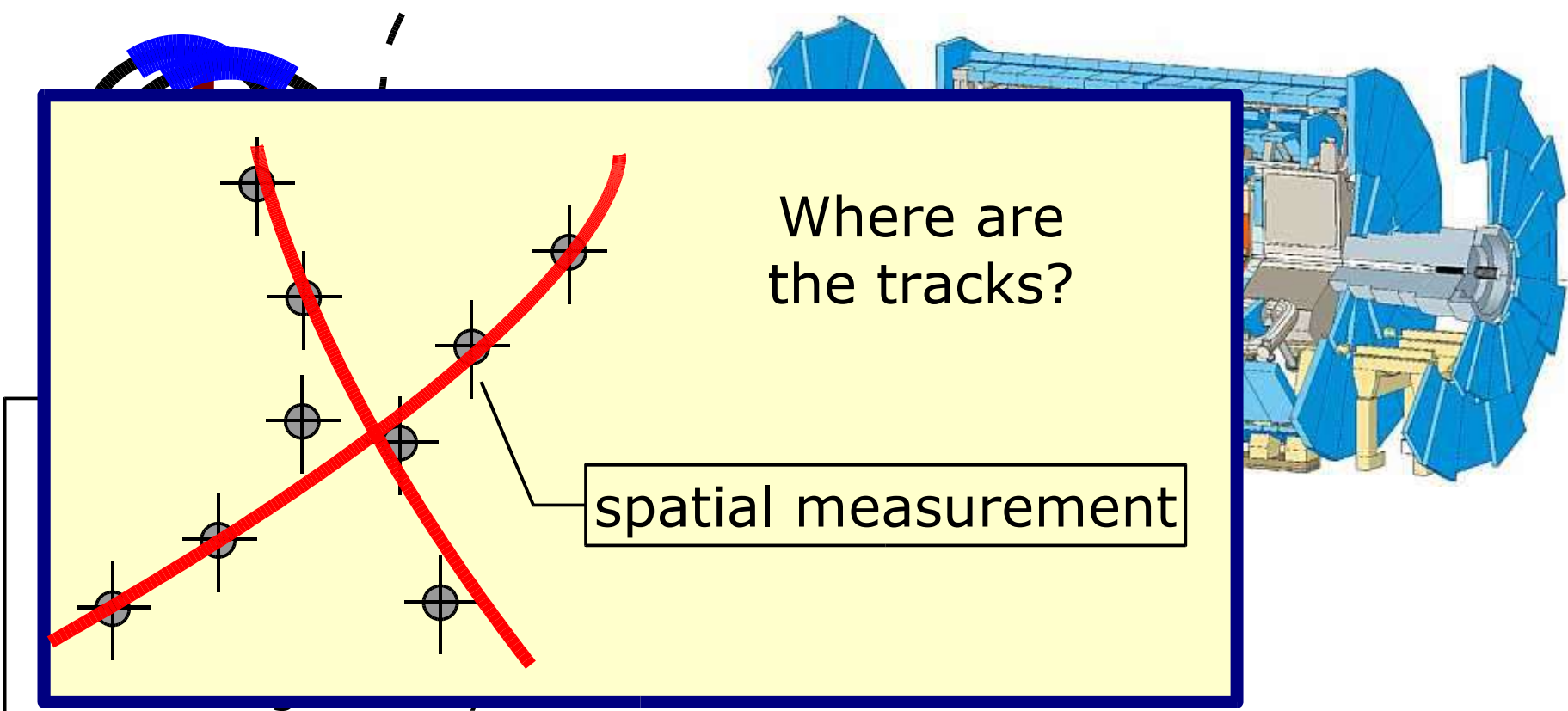
Where are
the tracks?

spatial measurement

- choice of sub-detectors (physical properties, deterioration, ..)
- event type
- trigger efficiencies
- reconstruction & analysis algorithms / SW & computing

How can we build a detector, that is "efficient" enough
to measure what we want to measure?

=> simulation studies contribute significantly
to the taken decisions



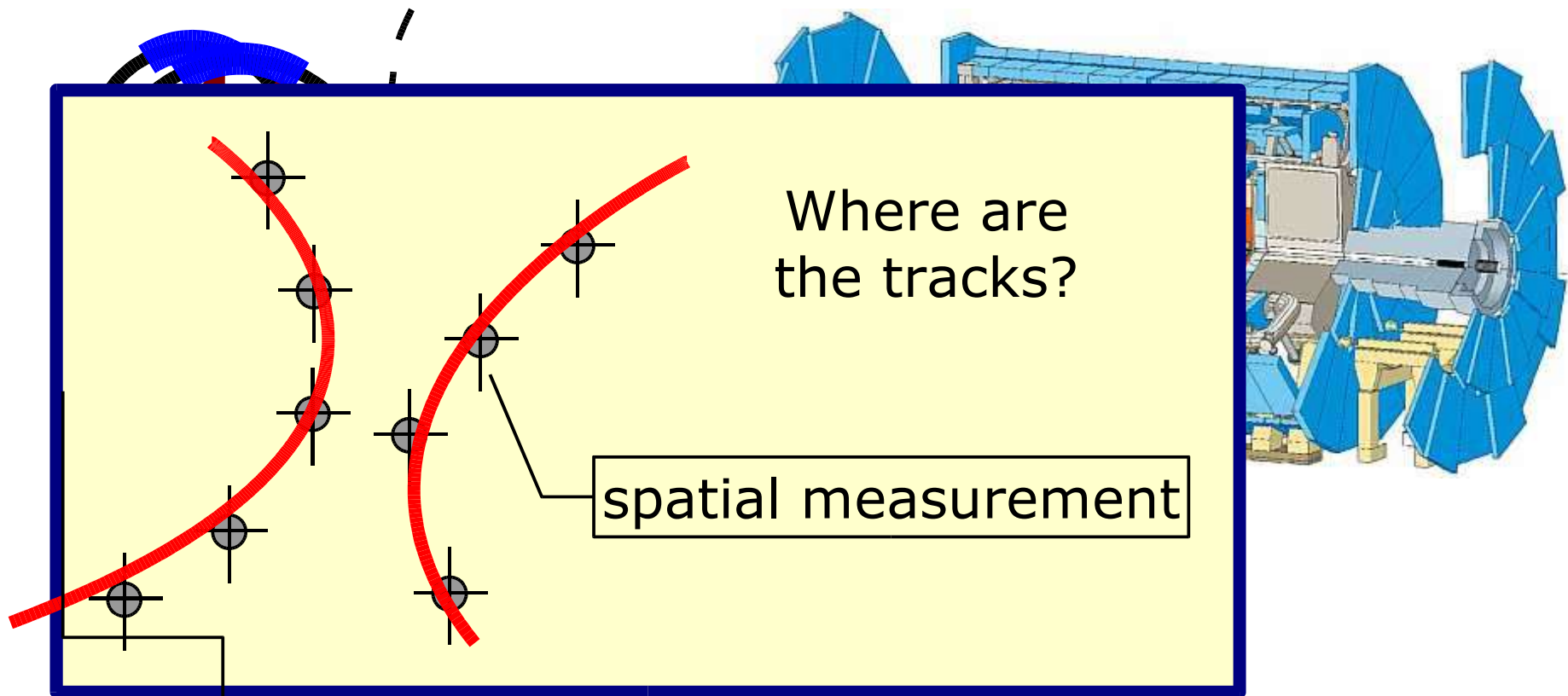
Where are the tracks?

spatial measurement

- choice of sub-detectors (physical properties, deterioration, ..)
- event type
- trigger efficiencies
- reconstruction & analysis algorithms / SW & computing

How can we build a detector, that is "efficient" enough to measure what we want to measure?

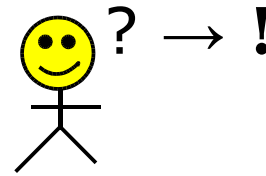
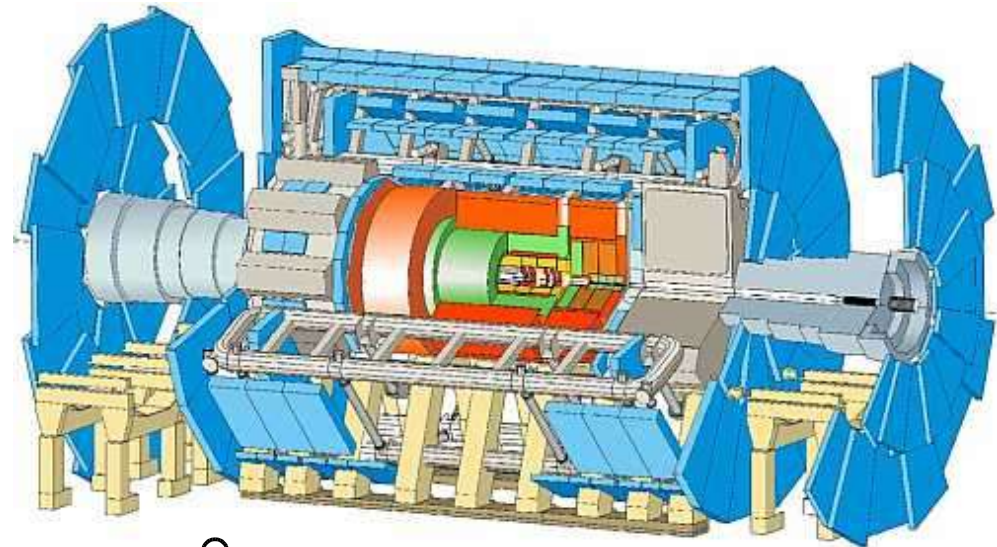
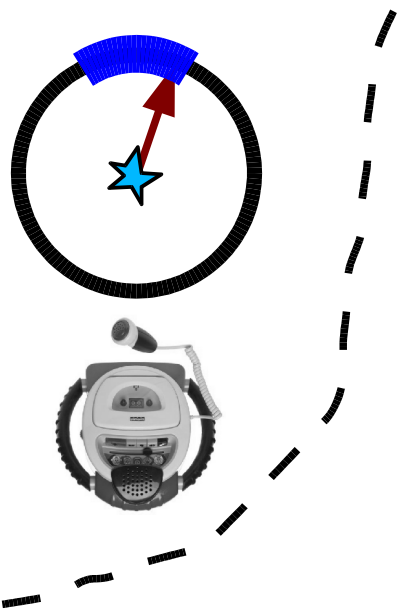
=> simulation studies contribute significantly to the taken decisions



- choice of sub-detectors (physical properties, deterioration, ..)
- event type
- trigger efficiencies
- reconstruction & analysis algorithms / SW & computing

How can we build a detector, that is "efficient" enough to measure what we want to measure?

=> simulation studies contribute significantly to the taken decisions



Experiment simulations help to

- design & understand the detector and its data
- verify, train, optimize the event selection (triggering)
- verify, train, optimize the algorithms to reconstruct the physics events from the data

Some thoughts about noise and background ..

- What 's the signal to noise ratio
 - assuming a given theory to be tested?
 - \sim how many signal events, how many background and min. bias events?

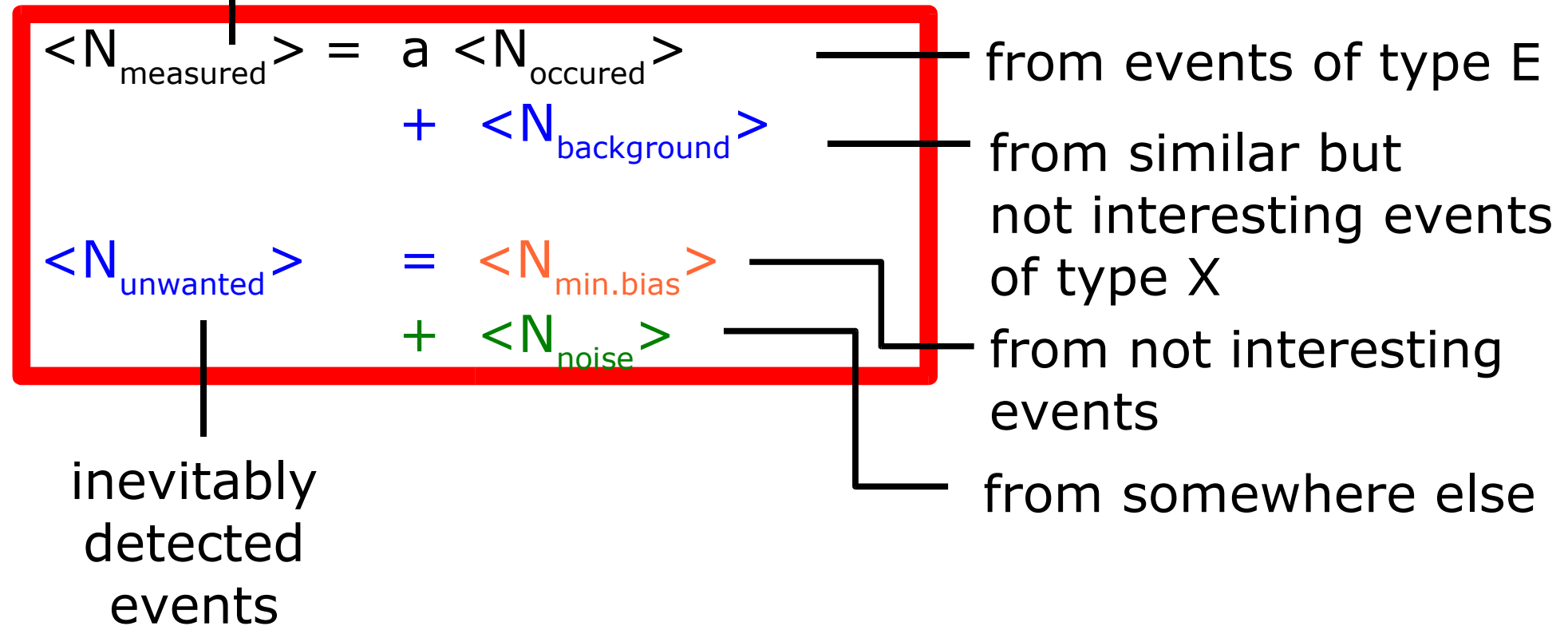
In other words: all the additional, unwanted crap being registered in the detector ...

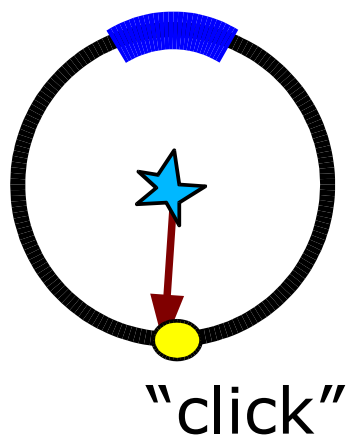
How to split simulation tasks to study these issues ...

Usually, we measure not only the signal!

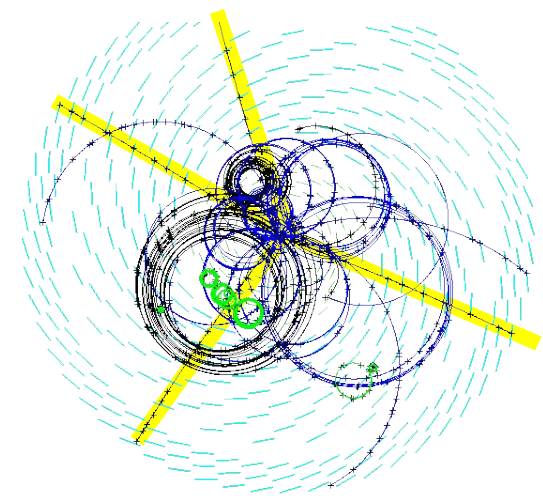
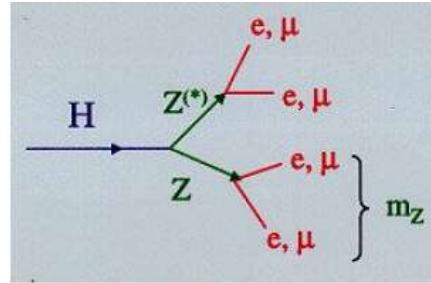
BACKGROUND distorting the measurement!

measured events
looking like events
of type E

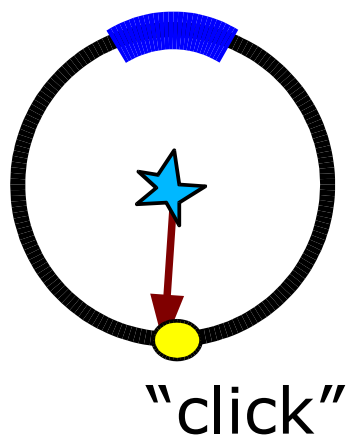




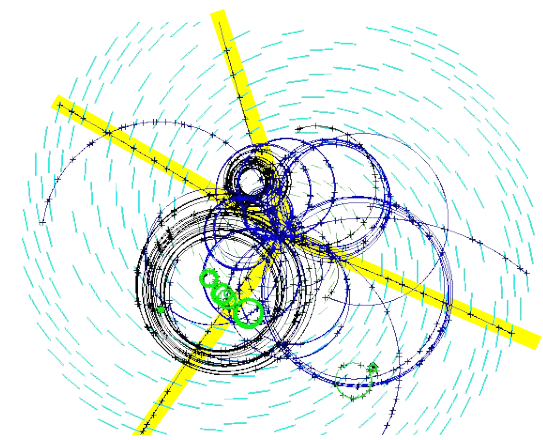
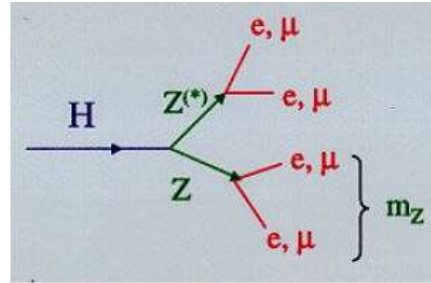
Signal



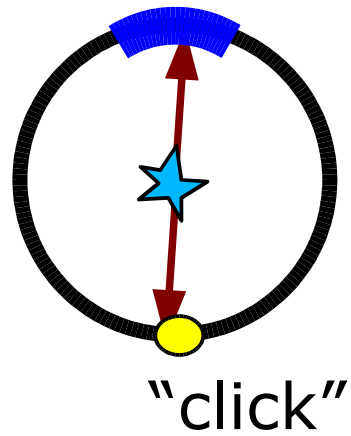
What we wish to measure!



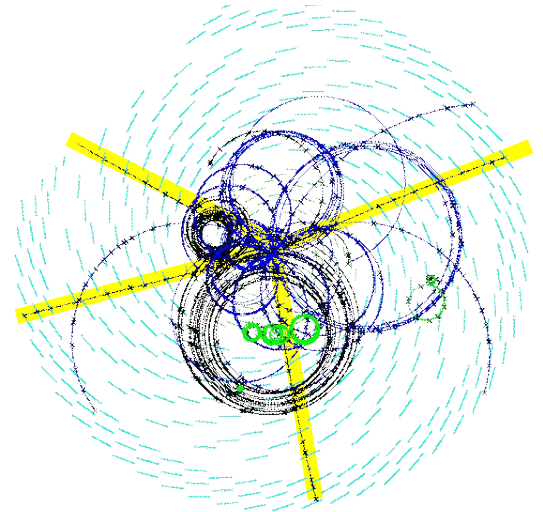
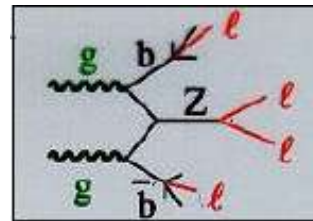
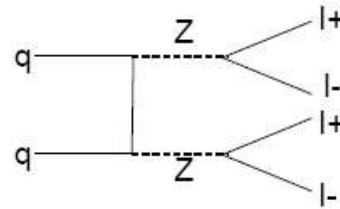
Signal

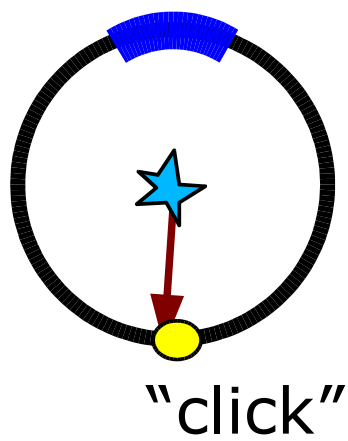


+ What we actually measure ...

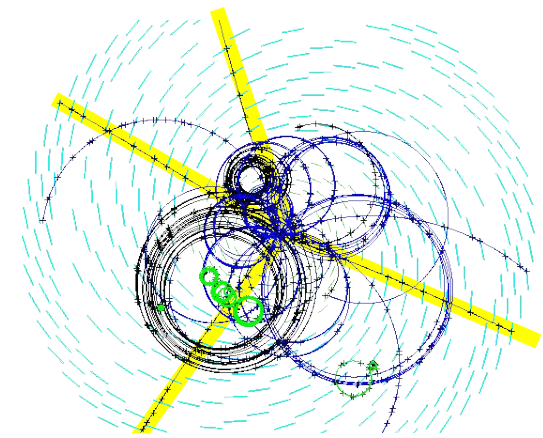
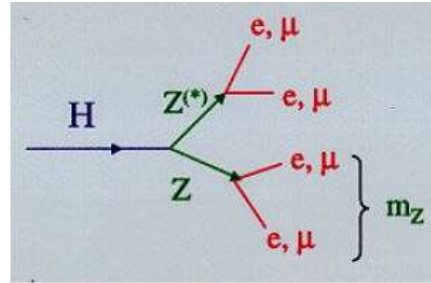


Back-ground

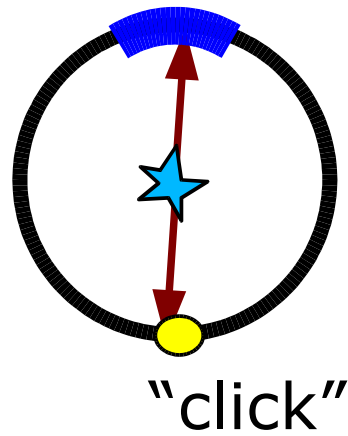




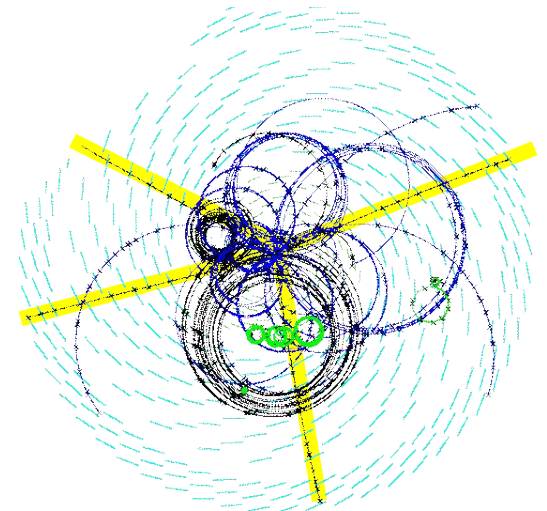
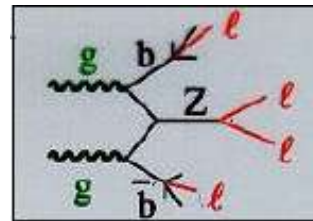
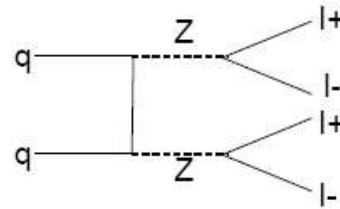
Signal



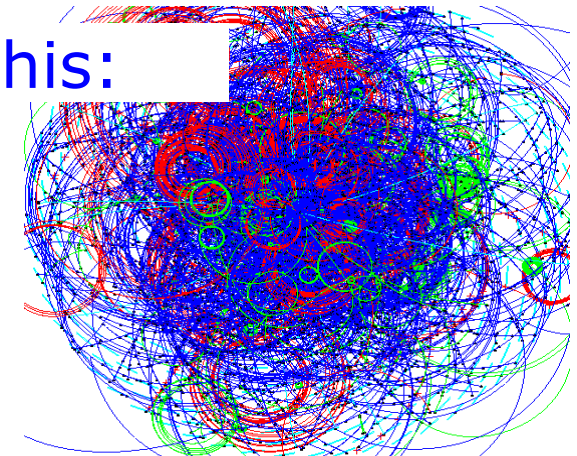
+ What we actually measure ...



Back-ground



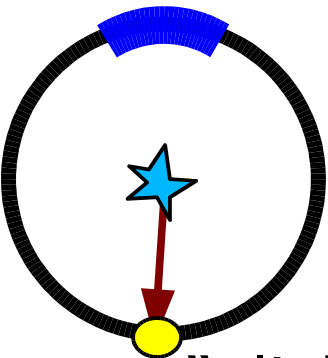
... if we manage to ignore this:



Mickey was lucky!

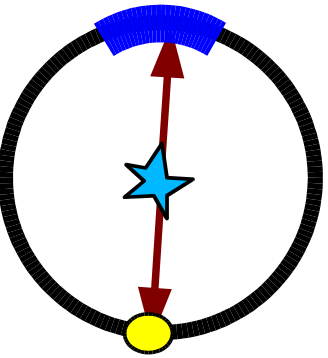
= minimal bias events and noise data

The four types of data



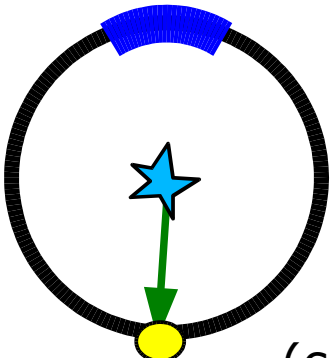
Signal

"click"



Back-ground

"click"



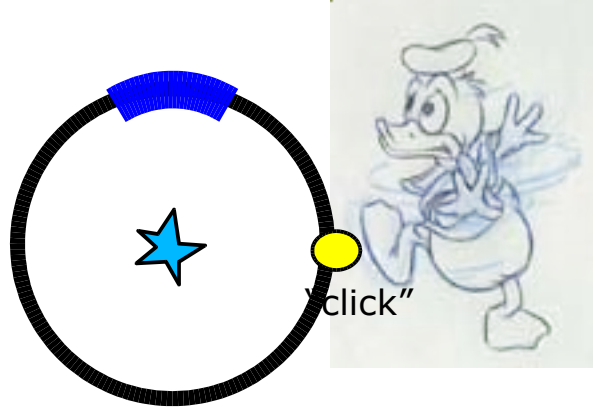
Minimal bias

emission of a "Pianissimon"

"click"

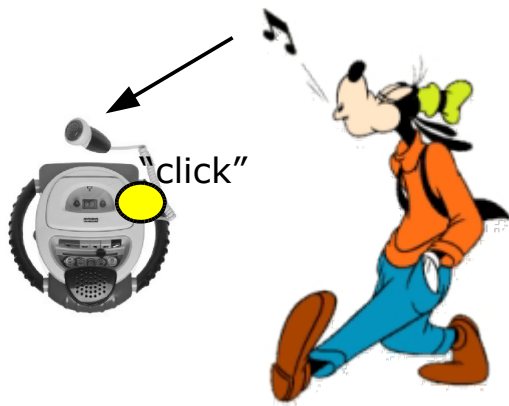
(comes from the interaction, but is not signal nor background)

Noise



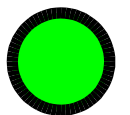
"click"

(comes from somewhere else)

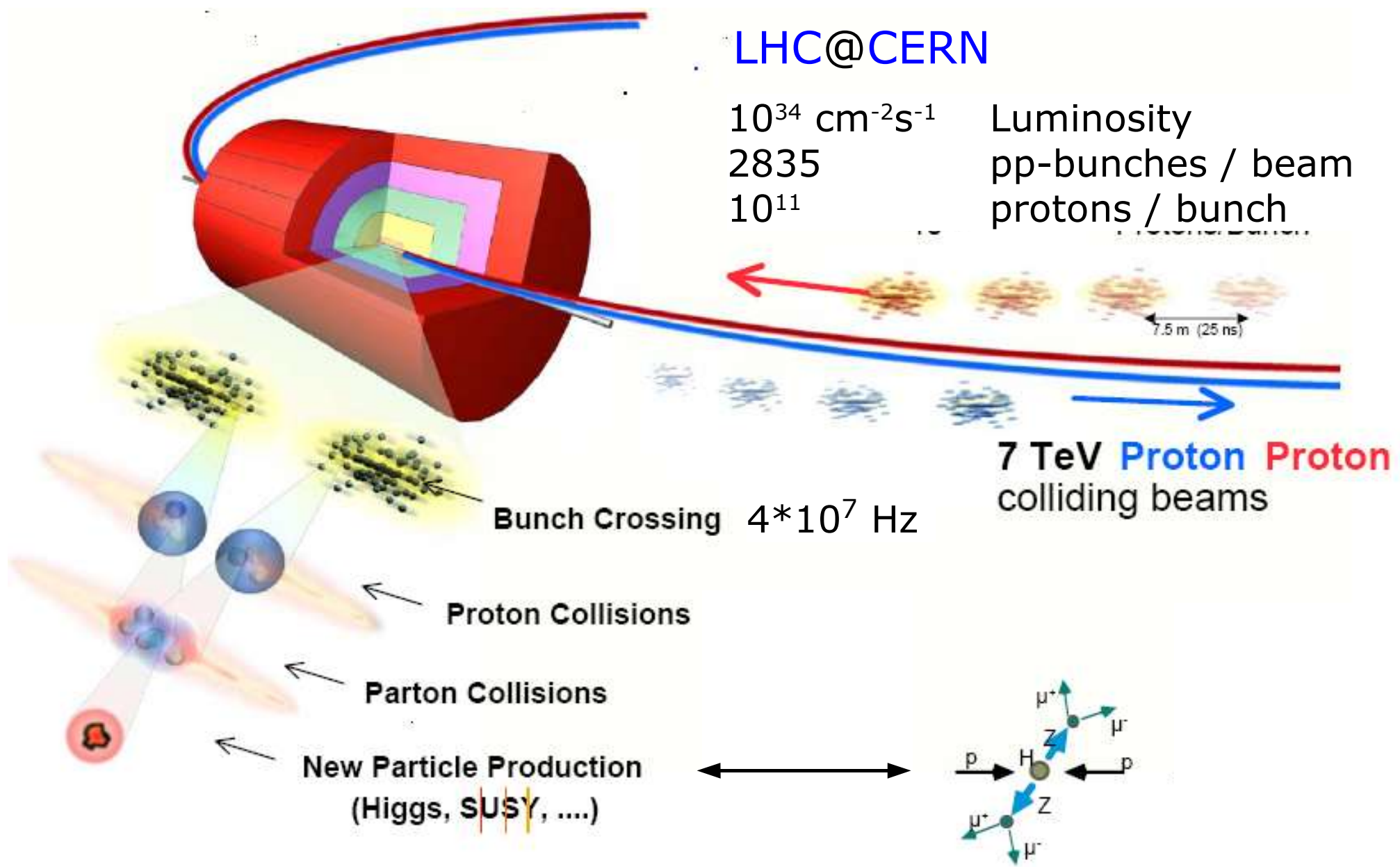


Let's see this for [LHC@CERN!](#)

... want to get a feeling of orders of magnitude for signal and background events, to see, why accurate simulations studies are required!



Rare and exotic birds ...



Very simple formula:

luminosity ($\text{cm}^{-2}\text{s}^{-1}$)

acceptance
($0 \leq a \leq 1$)

time (s)

number of
measured
events

$$N(T) = a \cdot \sigma \cdot \int L(t) \cdot dt$$

reaction cross section (cm^2)

number of events measured in the time interval $[0, T]$

(ignoring background ..)

- σ ... cross section: measures the interaction strength of two colliding particles; it depends on the physics nature of the particle collision
- L ... Luminosity: measures the crossing rate and beam density; it depends on the accelerator design

luminosity ($\text{cm}^{-2}\text{s}^{-1}$)

$$N(T) = a \cdot \sigma \cdot \int L(t) \cdot dt$$

reaction cross section (cm^2)

number of events measured in the time interval $[0, T]$

Interaction Rate

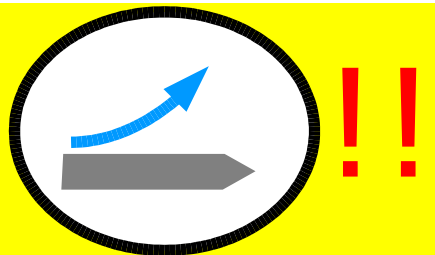
Simply get the time derivative of the number of events!

$$\frac{dN(t)}{dt} = \sigma \cdot L(t)$$

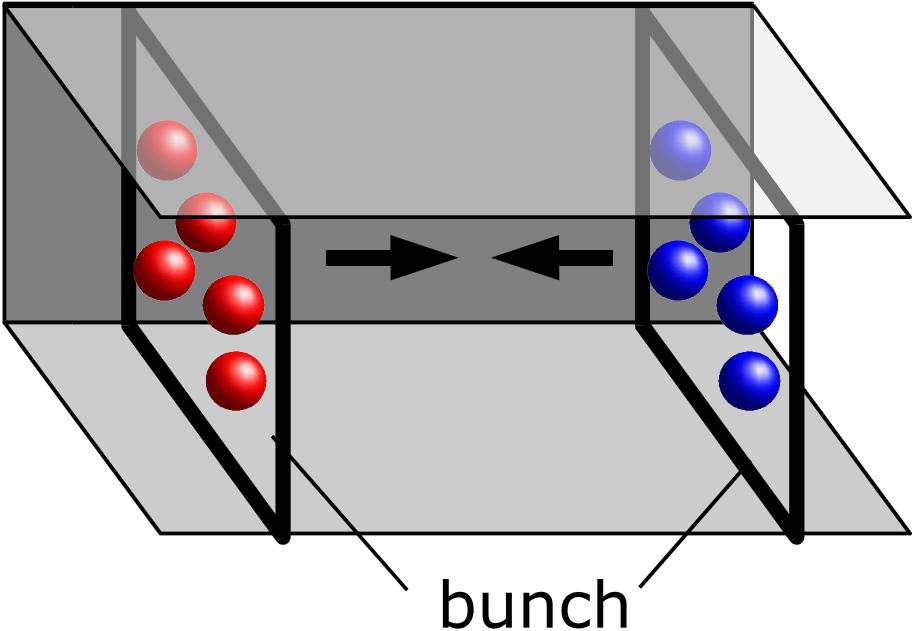
luminosity ($\text{cm}^{-2}\text{s}^{-1}$)

reaction cross section (cm^2)

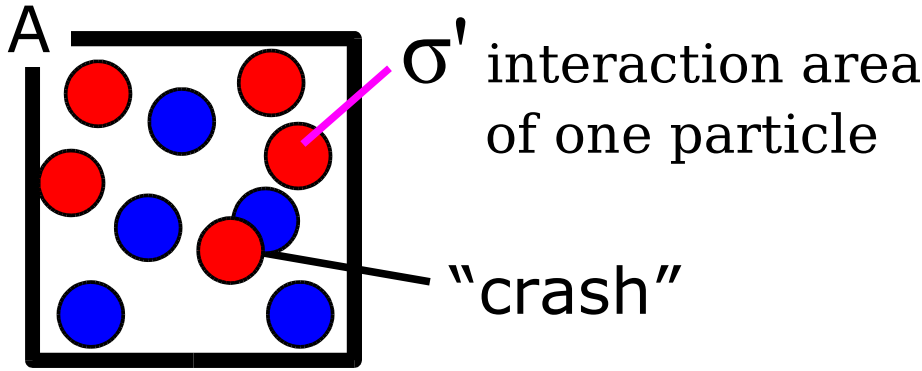
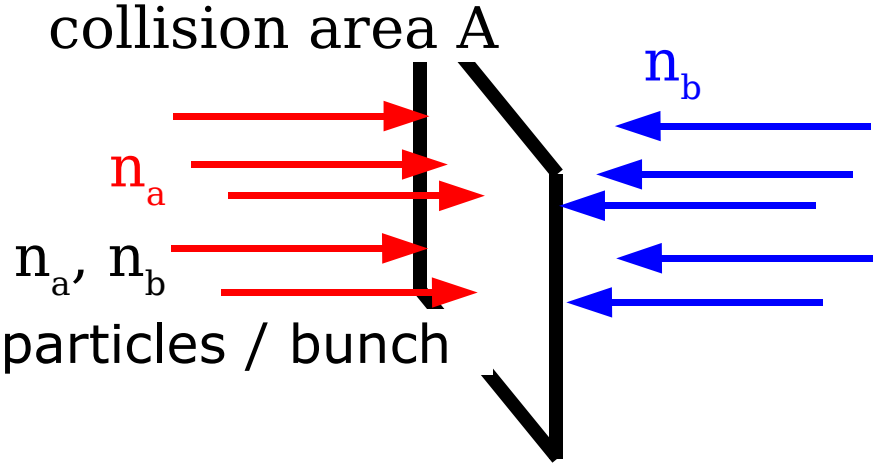
frequency: number of interactions per second

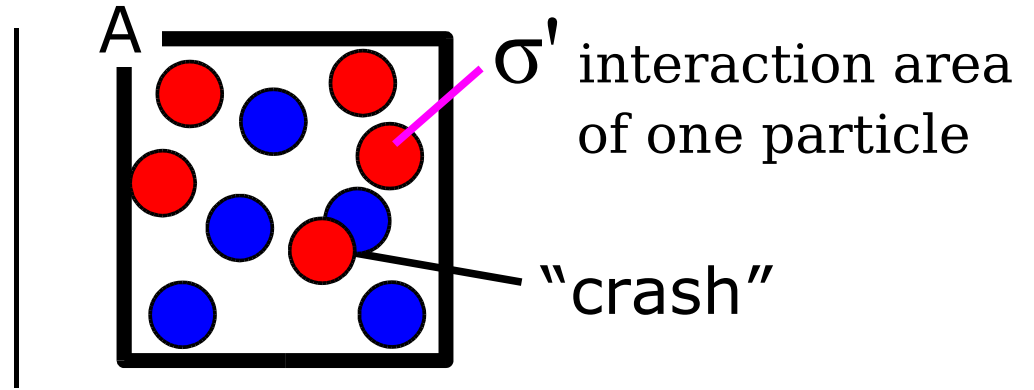
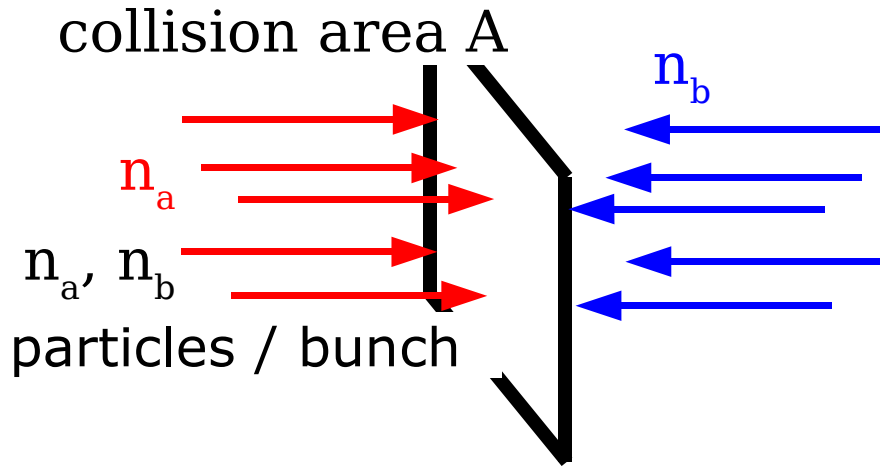


Let's look at one LHC bunch crossing:

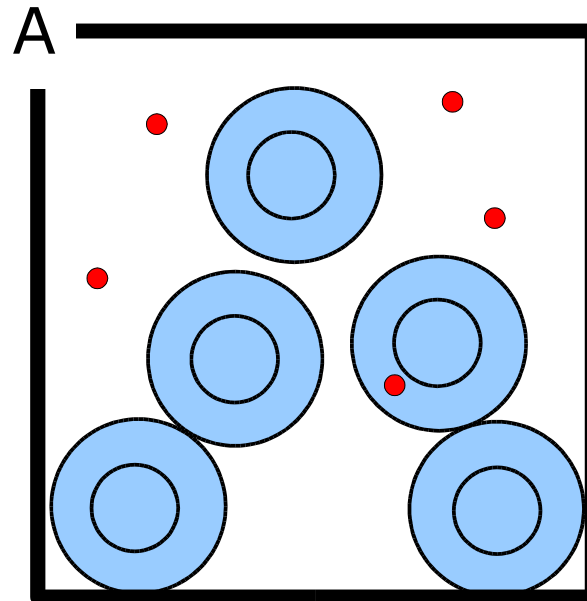
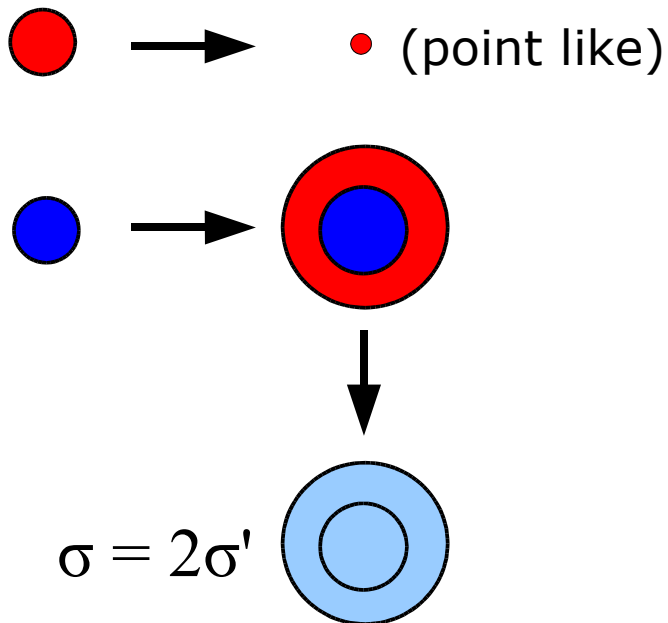


simplification:
all protons of one
bunch considered
to be in the same
plane



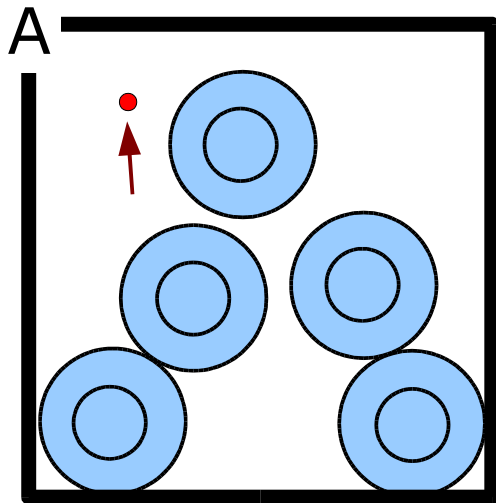


equivalent:



$\sigma = 2\sigma'$ interaction area for a two particle interaction

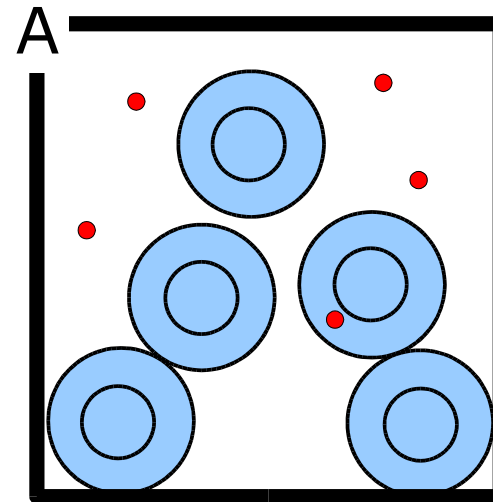
$n_b \cdot \sigma$... total interaction area in one bunch crossing



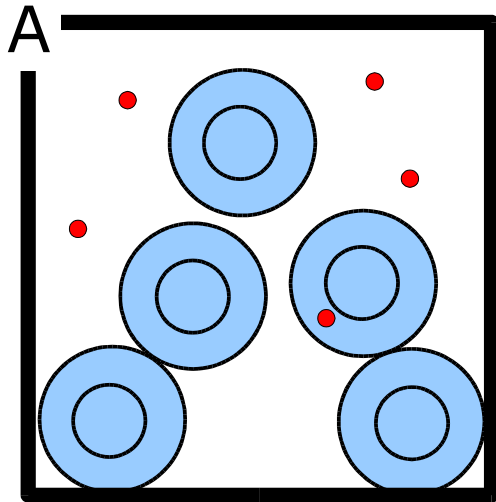
average number of collisions with n_a red particles in one bunch crossing is:

$$n = n_a \cdot w = n_a \cdot n_b \cdot \sigma / A$$

$n_b \cdot \sigma / A$... probability w , that **one red particle** will interact with **a blue particle** in one bunch crossing

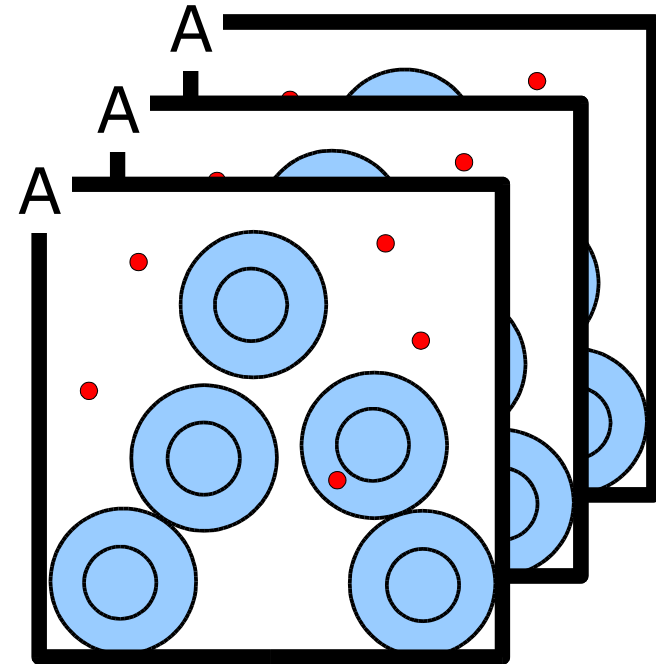


we have f bunch crossings per second:



$$n = n_a \cdot w = n_a \cdot n_b \cdot \sigma / A$$

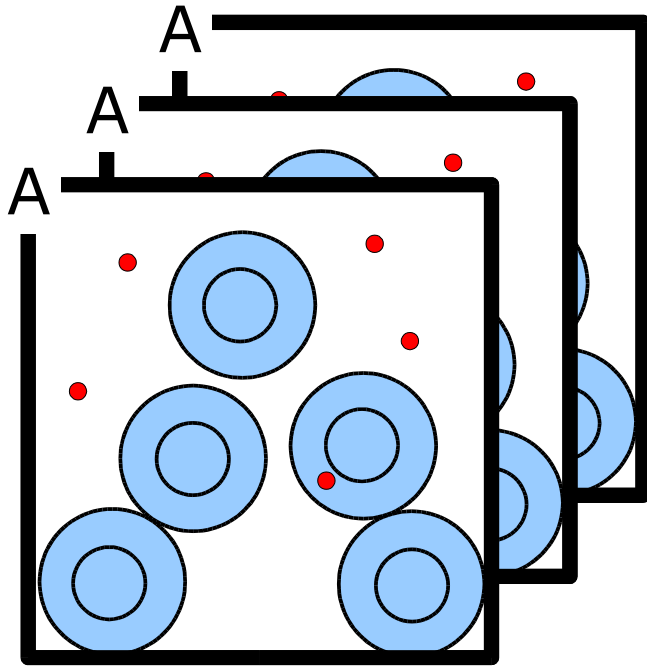
avg. number of interactions per bunch crossing



Interaction rate:

$$\frac{d n(t)}{d t} = f \cdot n_a \cdot w = \sigma \cdot \underbrace{f \cdot n_a \cdot n_b / A}_{\text{luminosity}}$$

$$= \sigma \cdot L$$



Interaction rate:

$$\frac{d n(t)}{d t} = f \cdot n_a \cdot w = f \cdot n_a \cdot n_b \cdot \sigma / A$$

= $\sigma \cdot L$, factorization
into physics & beam

Luminosity:

$$L = f \cdot n_a \cdot n_b / A$$

defined by beam
properties only!

$$N'(t) = \sigma \cdot \int L(t) \cdot dt$$

$$= \sigma \cdot L \cdot t$$

Number of interactions in
the time interval (0, t).

$$N(t) = a \cdot N'(t)$$

|
acceptance

Number of observed
interactions in the
time interval (0, t).

LHC@CERN:

$$n_a = n_b \sim 10^{11} \text{ protons/bunch}$$

Luminosity:

$$L = f \cdot n_a \cdot n_b / A$$

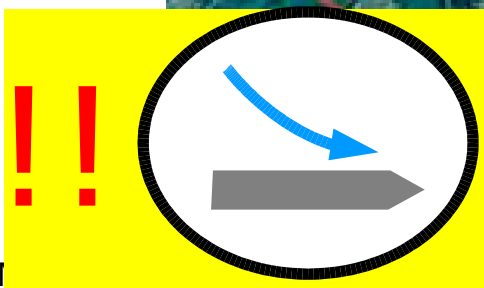
$$f = 40 \text{ MHz}$$
$$= 40 \cdot 10^6 \text{ Hz}$$

$$L = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

\sim
9km

$\sim 2 \times 3000$ bunches
in the ring

25ns time
btw. collisions



Cross Section(s)

Remember? interaction rate: $\frac{d n(t)}{d t} = \sigma \cdot L$
 σ ... total interaction cross section (cm², barn, ..)

well known processes

$$\sigma = \sigma_1 + \sigma_2 + \dots + \sigma_{\text{Higgs}}$$

unknown

yet undetermined process(es)

$$\sigma_x = \sigma_x(E, m, \text{"theory"}, \dots)$$

Remember: theories have unknown parameters

Theory → Observables → Experiment → Analysis
 (a, b, ..)

Theories have unknown parameters

Theory \rightarrow Observables \rightarrow Experiment \rightarrow Analysis
(a, b, ..)

$$\sigma_x = \sigma_x(E, m, \text{"theory"}, \dots)$$

In HEP, these parameters are determined by the same experiment that should verify/falsify the theory!!

Parameters also mean: experiments must work accurate over the possible ranges of these parameters.

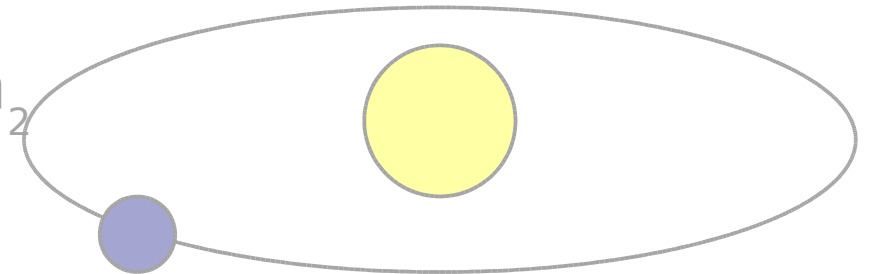
Classical example:

$$F_g = G \frac{m_1 m_2}{r^2}$$

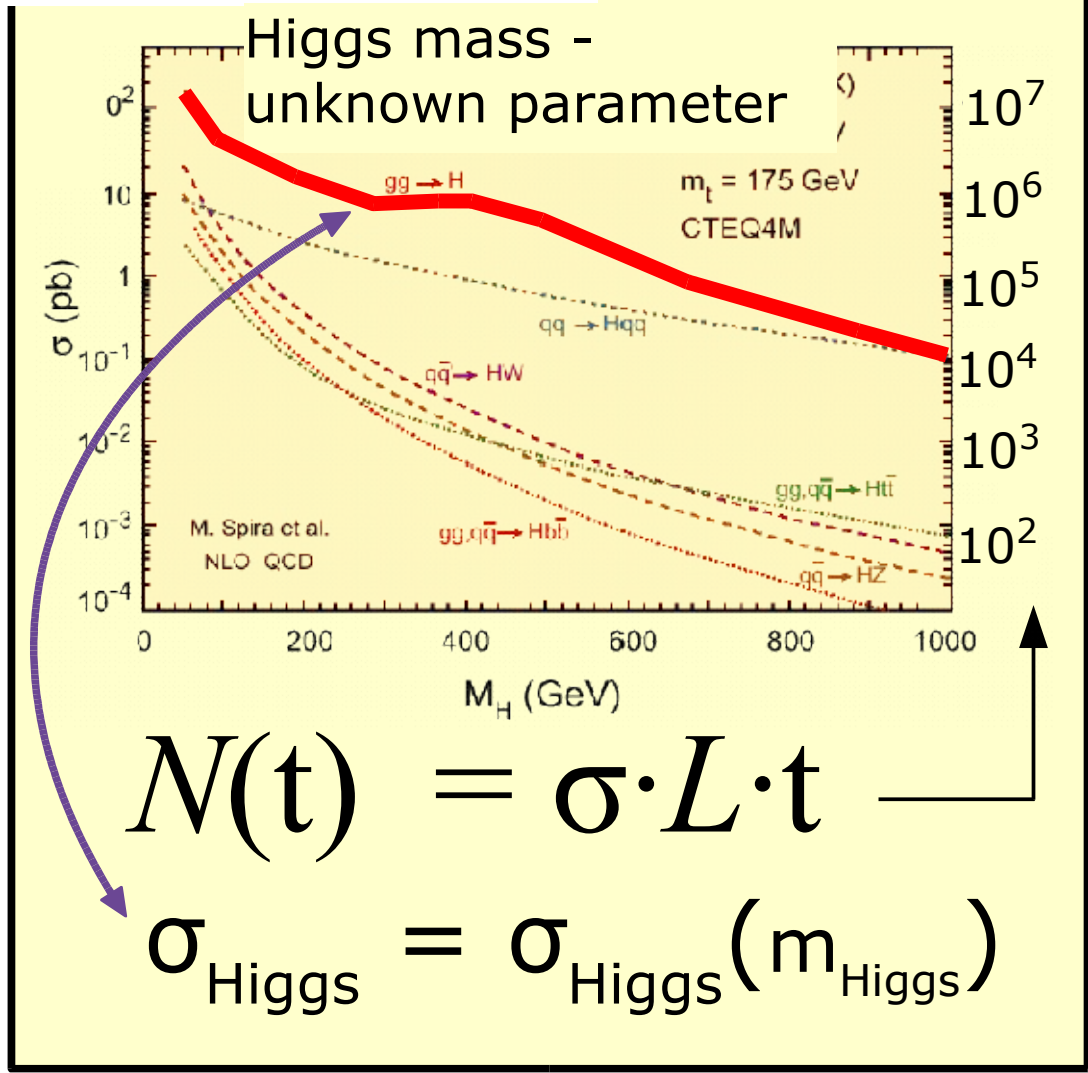
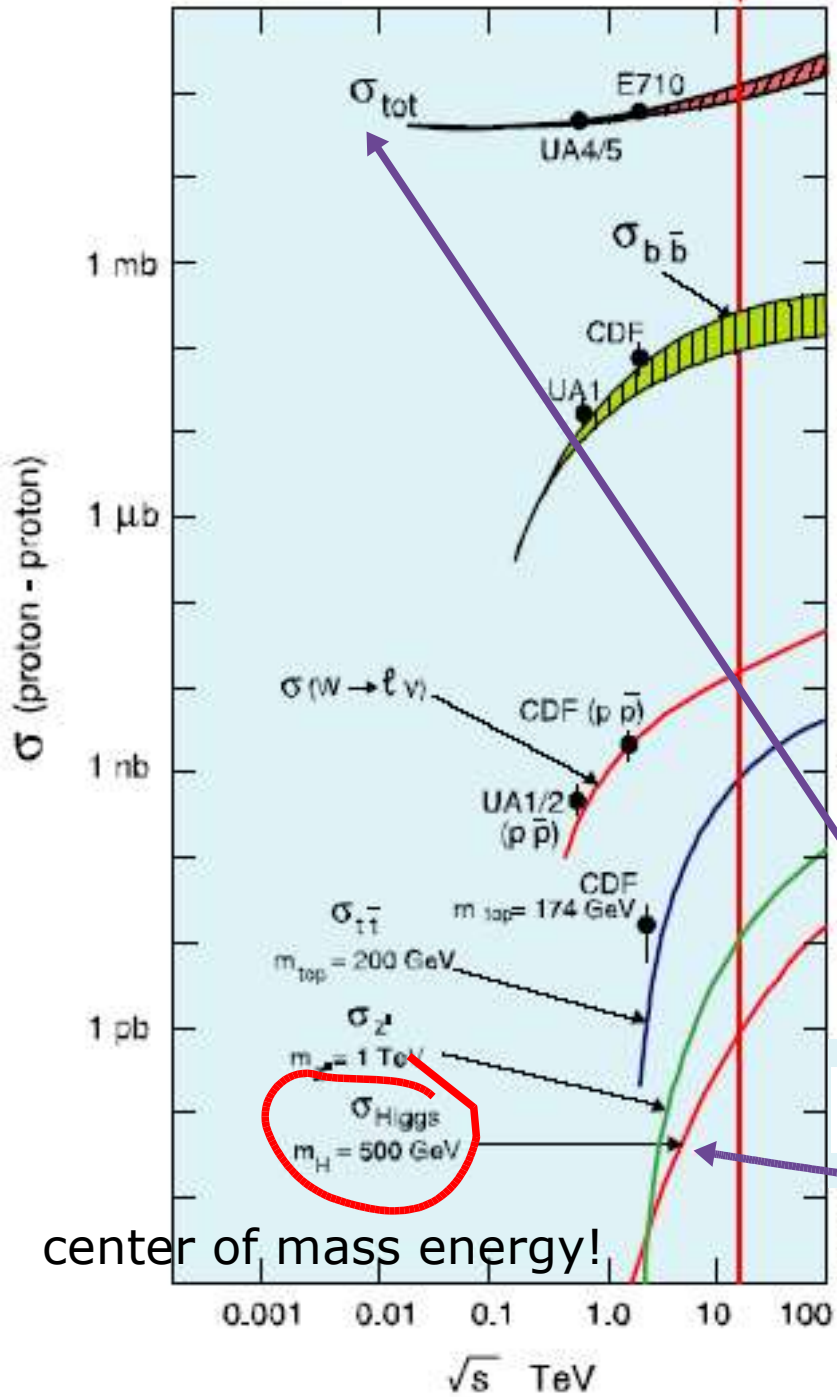
Parameters: G, m_1, m_2

Observables:
revolution time, path,
pendulum freq.

Experiments: pendulum, system earth-sun, moon-earth, ...



1 year LHC at highest L = $10^{34} \text{ cm}^{-2}\text{s}^{-1}$



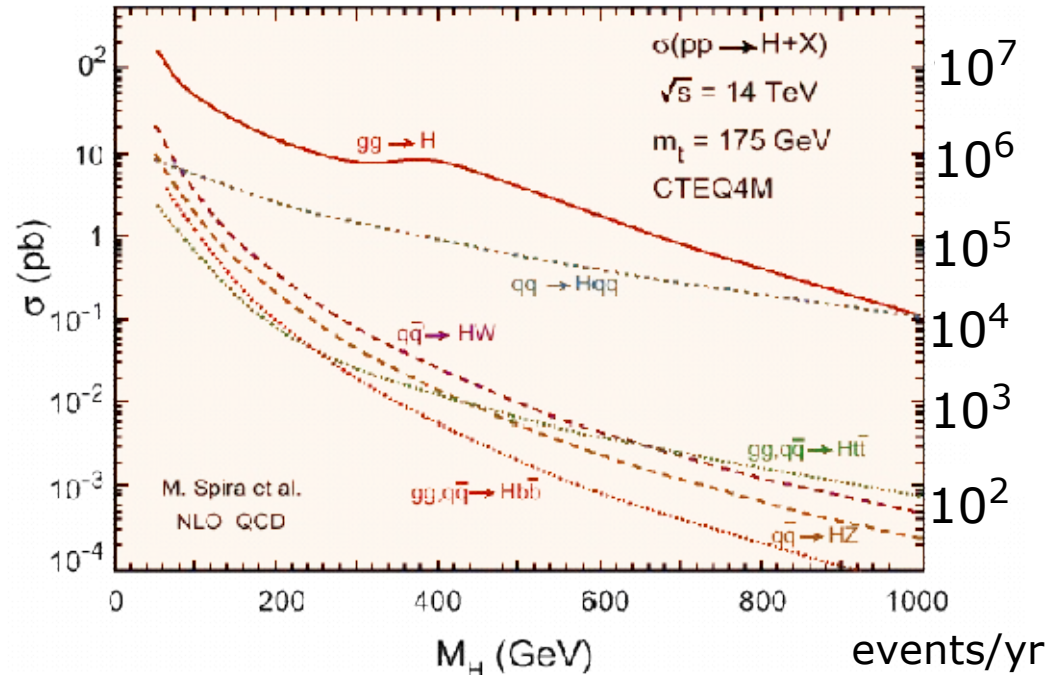
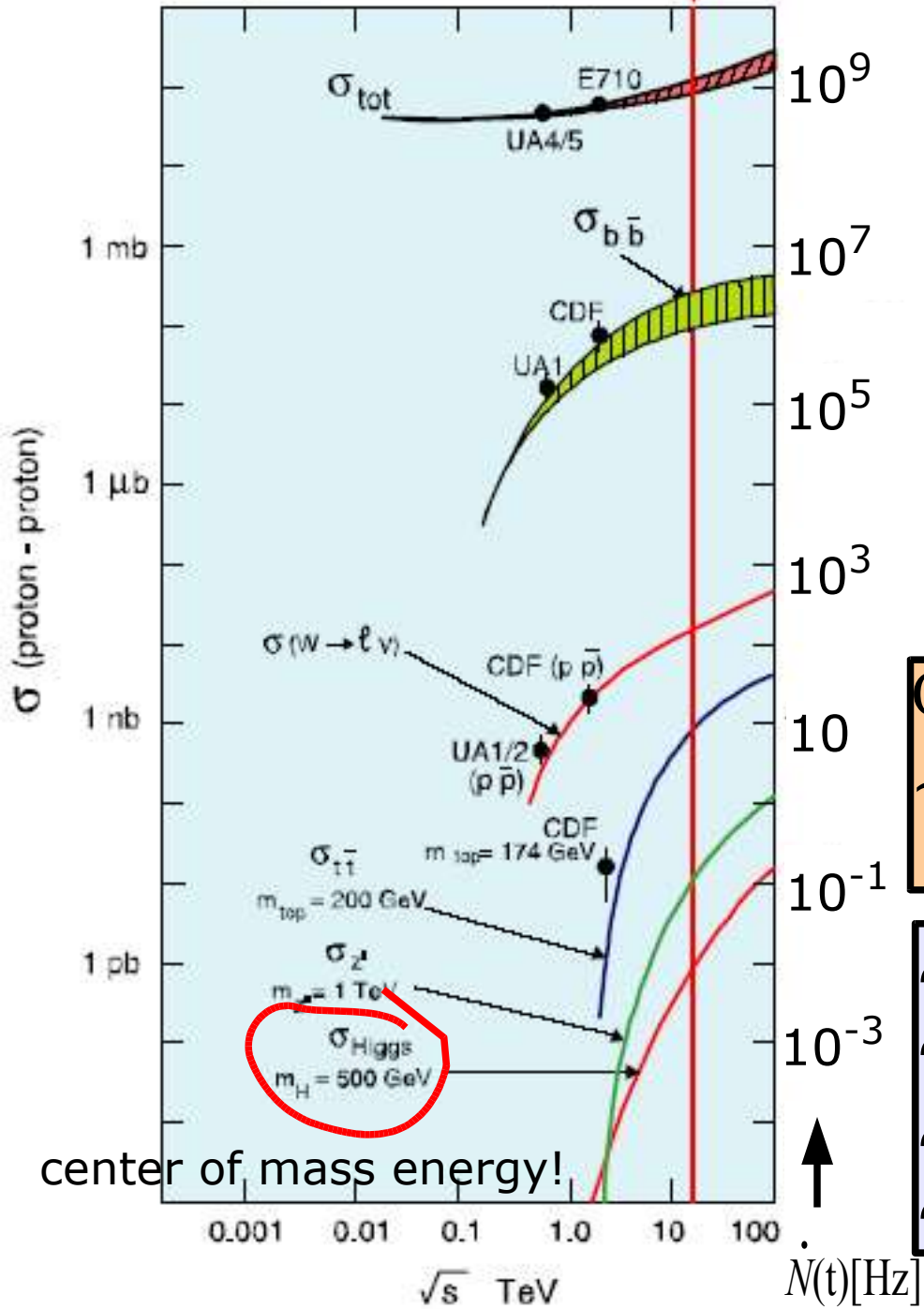
$$N(t) = \sigma \cdot L \cdot t$$

$$\sigma_{\text{Higgs}} = \sigma_{\text{Higgs}}(m_{\text{Higgs}})$$

$$\sigma = \sigma_1 + \sigma_2 + \dots + \sigma_{\text{Higgs}}$$

$$N(t)[\text{Hz}] = \sigma \cdot L$$

1 year LHC at highest $L = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



Collisions of bunches a $\sim 3000p$:
 ~ 20 simultaneous interactions
 every 25ns!

$\sim 10^5$ Higgs / year
 $\sim 10^{16}$ something else / year
 ~ 0.01 Higgs per second
 $\sim 1.000.000.000$ Interactions/sec

Observables → Discovery

Because of the quantum character of the physics:

- we talk of event rates
- there is no such a thing than “single measurement of THE Higgs particle”

Count sufficiently enough events of (indirect) decay products of the particle looked for in as many decay channels as possible!

The count must be statistically significant compared to the background noise (5 sigma) to claim “discovery”.

To be really confident:

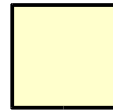
Discovery in many decay channels, in more than one experiment!

The “Truffles Pig”

$\sim 10^5$ Higgs / year
 $\sim 10^{16}$ something else /
year

→ **1** Higgs event in **10^{11}** events

1 event .. $1 \text{ dm}^2 = 10 \times 10 \text{ cm}^2$



10^{11} events .. $10^{11} \text{ dm}^2 \sim$
 $3 \cdot 10^5 \times 3 \cdot 10^5 \text{ dm}^2$



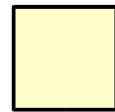
... just to visualize these numbers ...

The “Truffles Pig”

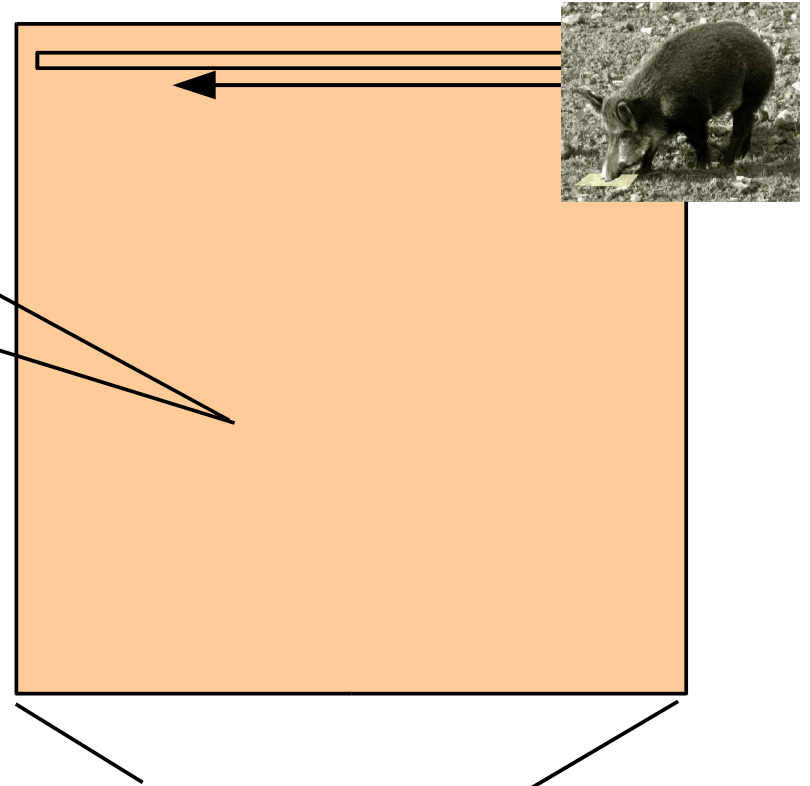
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→ **1** Higgs event in **10^{11}** events

1 event $10 \times 10 \text{ cm}^2$



10^{11} events .. $10^{11} \text{ dm}^2 \sim$
 $3 \cdot 10^5 \times 3 \cdot 10^5 \text{ dm}^2 =$
 $30 \times 30 \text{ km}^2 !!$



Find a **1 dm²** area in a square of **30 x 30 km²** !

(and search the area in ~ 1.5 minutes)

... and all this only if the Standard Model Higgs is “real”!

Experiments also search for evidence of other theories beyond the Standard Model:

- even more undefined parameters!!!

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Experiments also search for evidence of other theories beyond the Standard Model:

- even more undefined parameters!!!

Event Simulations (“Generators”)

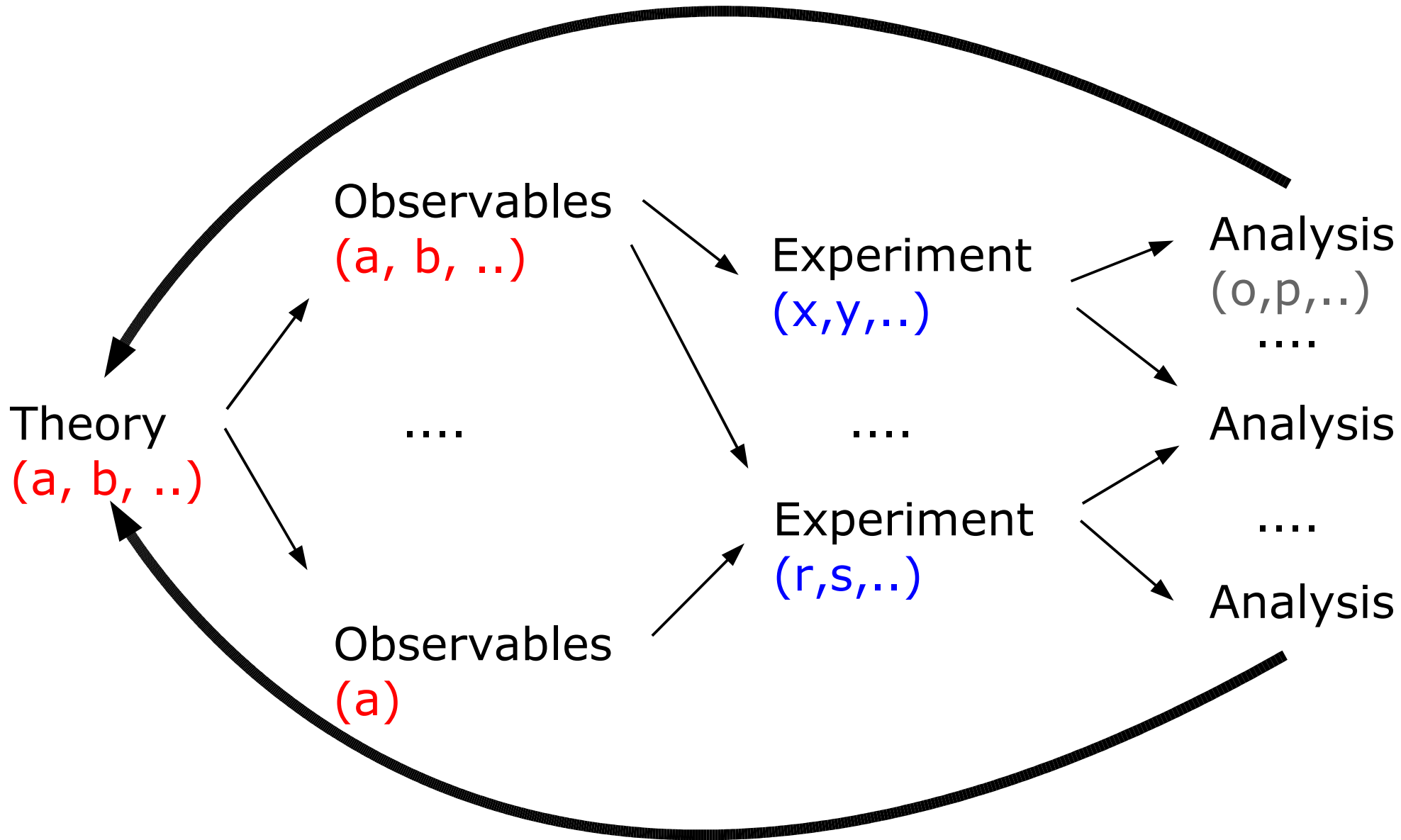
are used to generate amounts of samples of p-p collisions covering the parameter spaces of these theories!

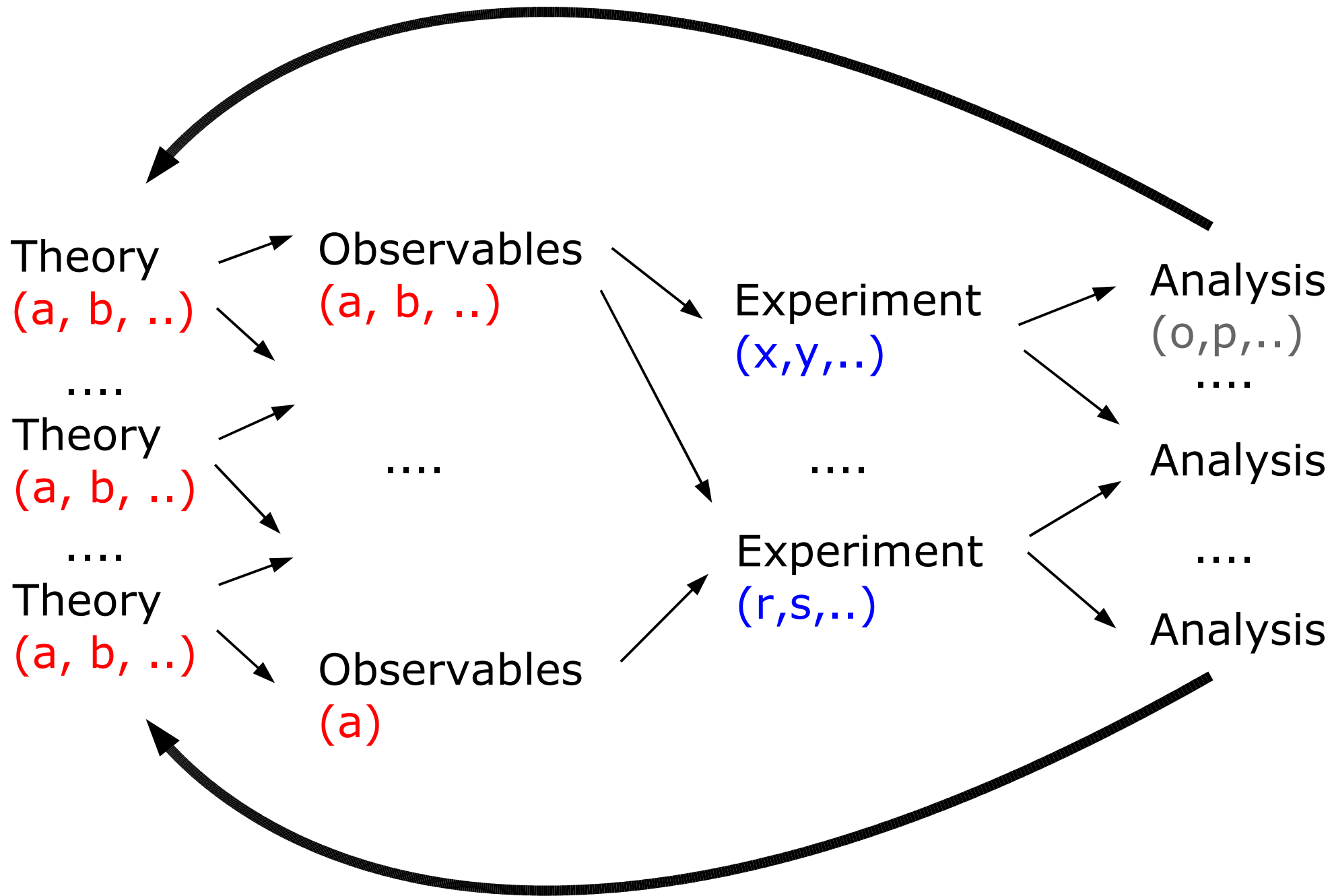
Special sampling methods are applied to correctly mix huge amounts of minimum bias events (“noise”) to all the various kinds of signal events

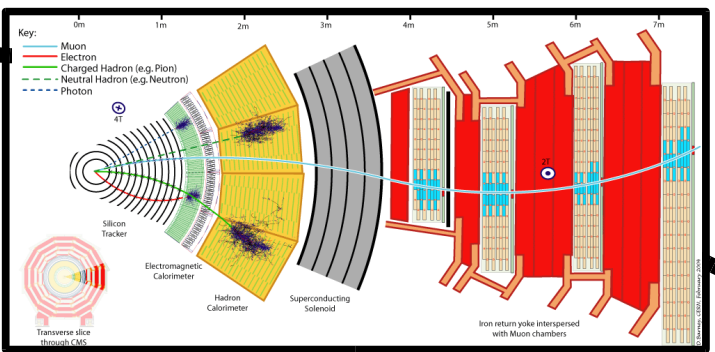
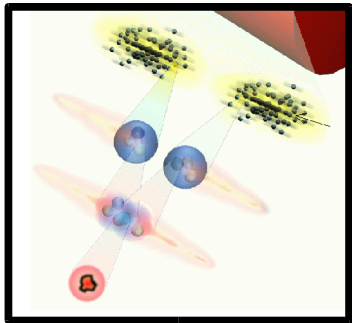
We won't cover Generators here ...

Simulation for ...

- Covering the parameter space of the physics theories to be tested in experiment
 - Various Generator codes exist
 - For LHC: quark-quark interactions up to 14 TeV center of mass energy
- Design, build, and understand detectors
 - Efficiency and acceptance calculations among various design options
 - Various levels:
 - Choice of “sensitive” material and geometrical layout – passage of particles through matter
 - Conversion of particle interactions to electronic measurement signals (ADC, TDC) and then physical quantities – digitization
 - Reconstruction of higher level physical objects (tracks, energy clusters, ...)







Theory
(a, b, ...)
Generator

Observables
(a, b, ..)

Exp. simulation

Experiment
(x, y, ...)

Analysis
(o, p, ...)

Theory
(a, b, ...)
Generator

....

Exp. simulation

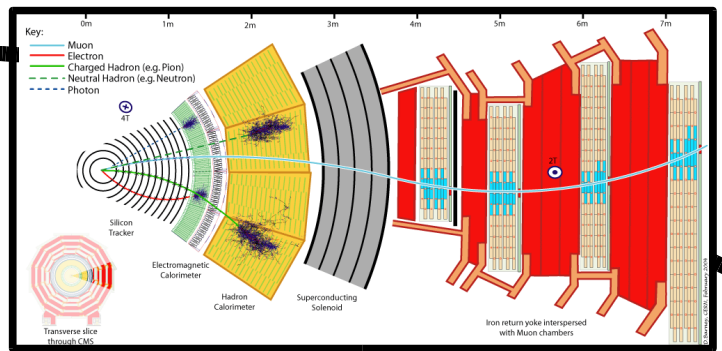
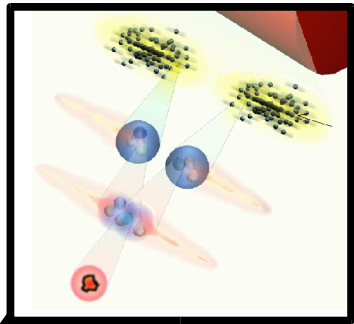
Experiment
(r, s, ...)

Analysis

Theory
(a, b, ...)
Generator

Observables
(a)

Analysis



Theory
(a, b, ...)
Generator

Theory
(a, b, ...)
Generator

Theory
(a, b, ...)
Generator

Observables
(a, b, ..)

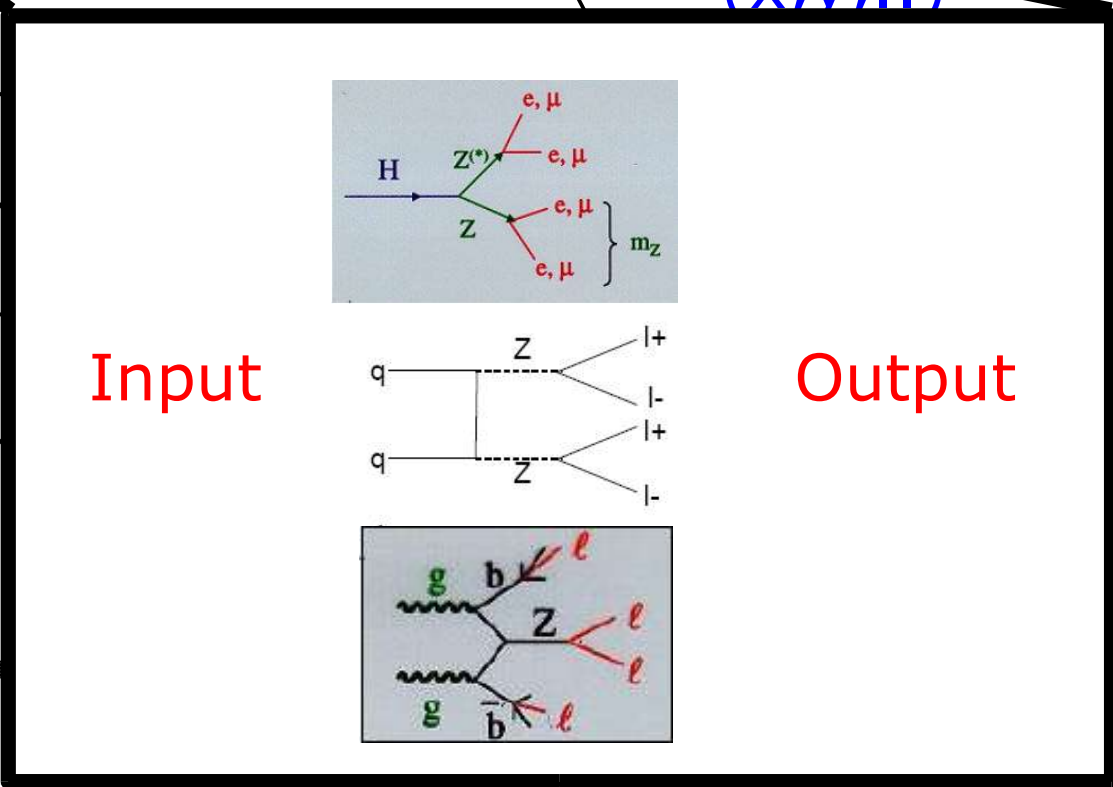
Exp. simulation

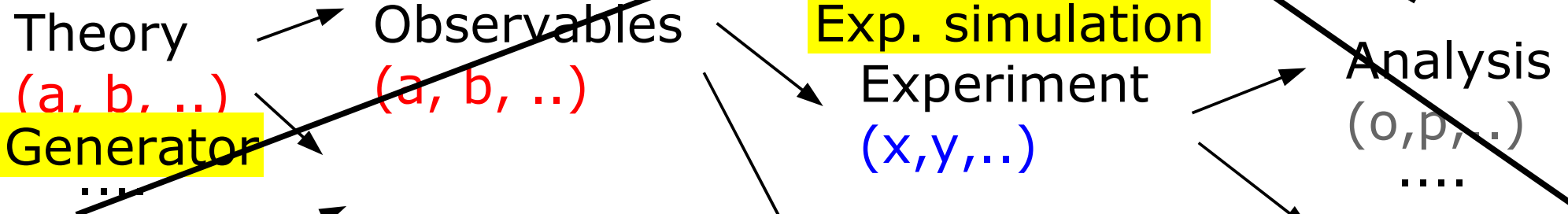
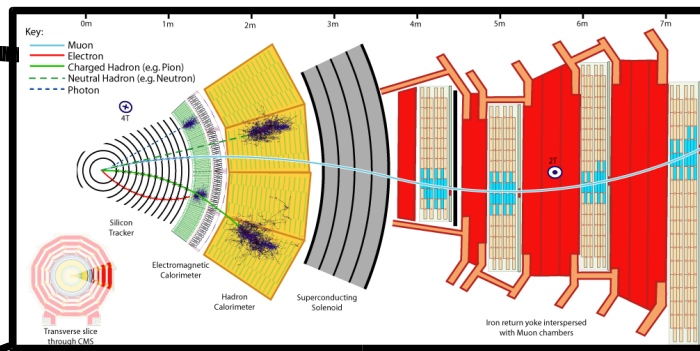
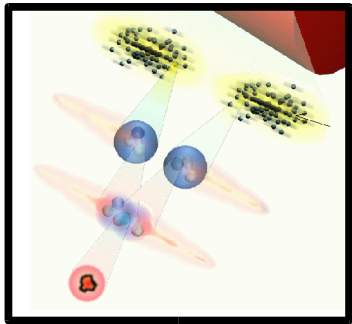
Experiment
(x, y, ...)

Analysis
(o, p, ...)

Analysis

Analysis





Th (a) Ge

Th (a) Ge

particle through matter simulation

A 3D visualization of a particle passing through a matter simulation. The particle is shown as a green line moving through a complex, multi-colored structure representing the matter. The colors range from yellow to purple.

+

Digitization

Three graphs labeled (a), (b), and (c) showing the digitization process. Graph (a) shows a smooth red curve representing the signal shape. Graph (b) shows the signal being sampled by electronics, with vertical lines indicating the sampling points. Graph (c) shows the resulting digitized signal, which is a blue curve with a red vertical line indicating a specific point of interest. The x-axis for all graphs is time t in units of 25 ns.

signal recorded by electronics
(not in these lectures, highly experiment specific)

GEANT4 – this lectures

What is GEANT4

“Geant4 is a toolkit for simulating the passage of particles through matter. It includes a complete range of functionality including tracking, geometry, physics models and hits.” [1]

[1] NIM A506 (2003), 250-303

GEANT comes from GEometry ANd Tracking.

The history of GEANT goes back to the 1970s (CERN)

Official homepage: <http://www.cern.ch/geant4>

Geant4 is the C++ successor of the FORTRAN Geant3 (and much more).

1994–1998: R&D phase, ~100 scientists from >10 experiments world wide;
first production release in 1998; today's (2005) release: GEANT4.7.1
=> more than 10 years of work!!

Areas of application: high energy physics, medical application, space science

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So, it's a Pop-Star! ;-)

(Pop ... particles over particles)

ch more).

Summary -1-

- **Need of simulation**
 - understanding the experiment
 - complexity of physics: generators
 - complexity of detectors:
 - passage of particles through matter (GEANT4)
 - response simulation (elect. measurement signals)
- **Basic design of a collision detector**
 - onion shell design, what is measured where
- **Concept of cross-section**
- **Types of data:**
 - signal and background
 - minimum bias events
 - noise